

# Joint Disparity and Optical Flow by Correspondence Growing

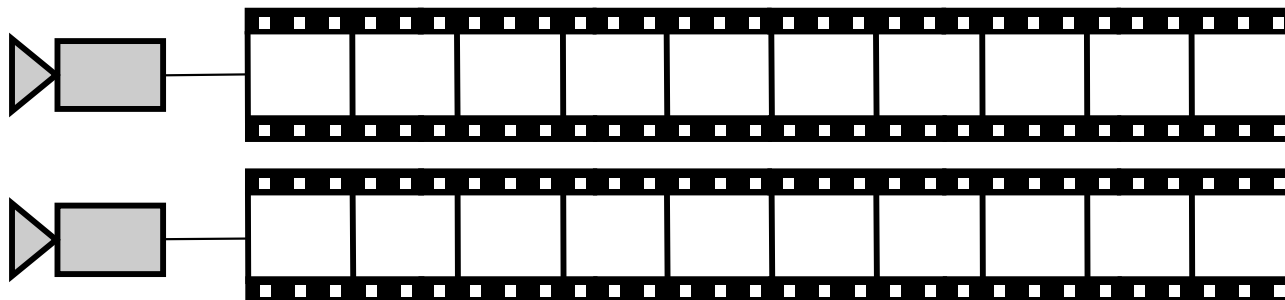


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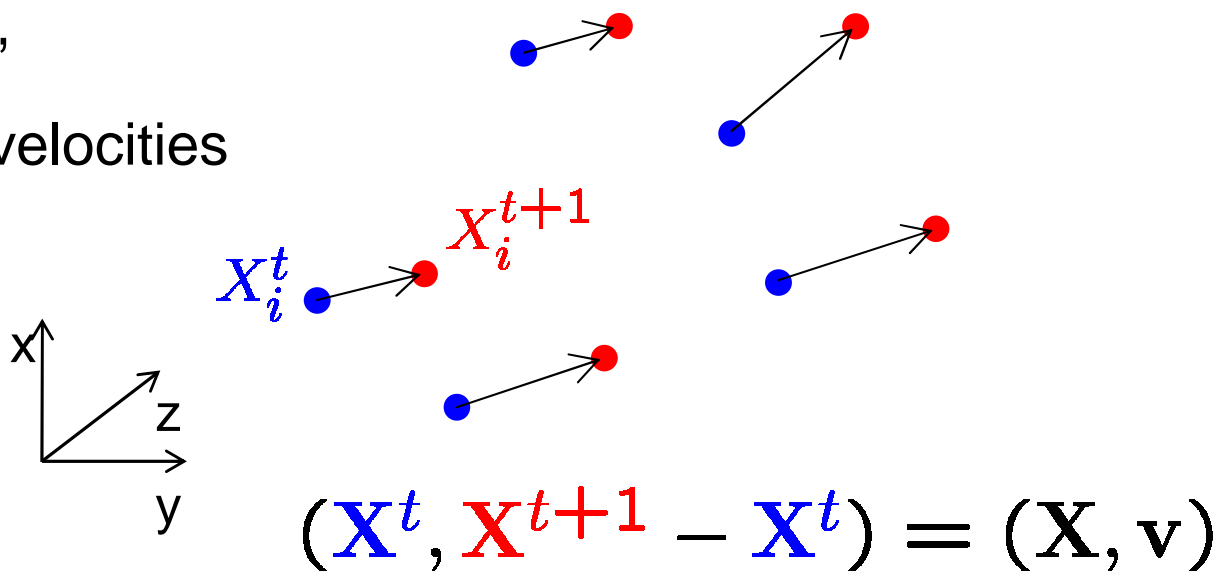
# Stereo Disparity and Optical Flow $\Rightarrow$ Scene Flow

**INPUT:** two stereo sequences from calibrated and synchronized cameras in a narrow baseline setup



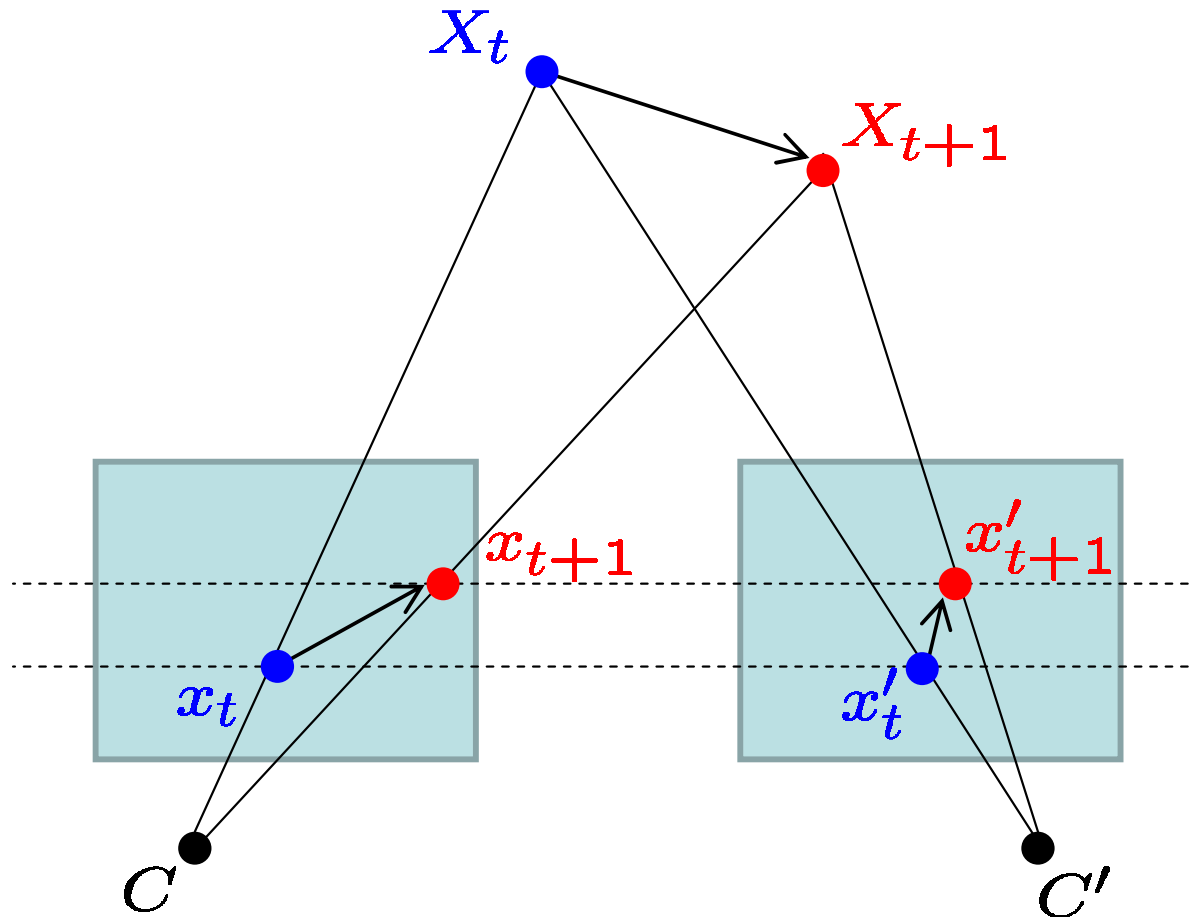
**OUTPUT:** disparity and optical flow maps  $\Rightarrow$  3D scene flow

- Scene flow = “motion field”
  - 3D scene points + 3D velocities



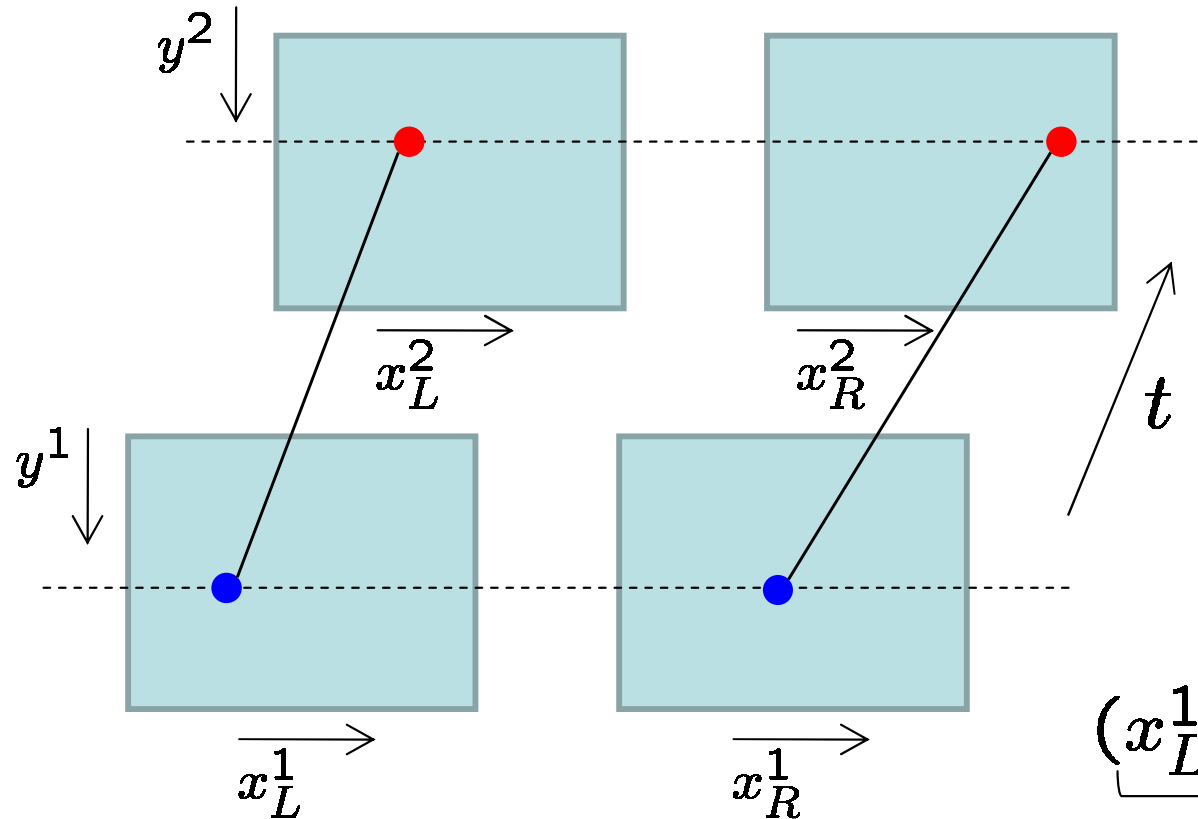
# Scene Flow Estimation

- Stereo disparity and optical flow – image correspondence problem
  - Assuming calibration of cameras  $\Rightarrow$  3D scene flow
- No assumptions on rigidity of the scene
- Camera static or moving  
(but stereo-rig geometry fixed, calibration known)



# Scene Flow Estimation

- The task: given  $X^t$ , find  $X^{t+1}$ 
  - Reconstruct as many points as possible



$$d^1 = x_L^1 - x_R^1$$

$$d^2 = x_L^2 - x_R^2$$

$$f_x = x_L^2 - x_L^1$$

$$f_y = y_L^2 - y_L^1$$

$$\underbrace{(x_L^1, x_R^1, y^1)}_{\rightarrow X^t}, \underbrace{(x_L^2, x_R^2, y^2)}_{\rightarrow X^{t+1}}$$

⇒ Stereo and optical flow problems constraint each other

# Example of the Results

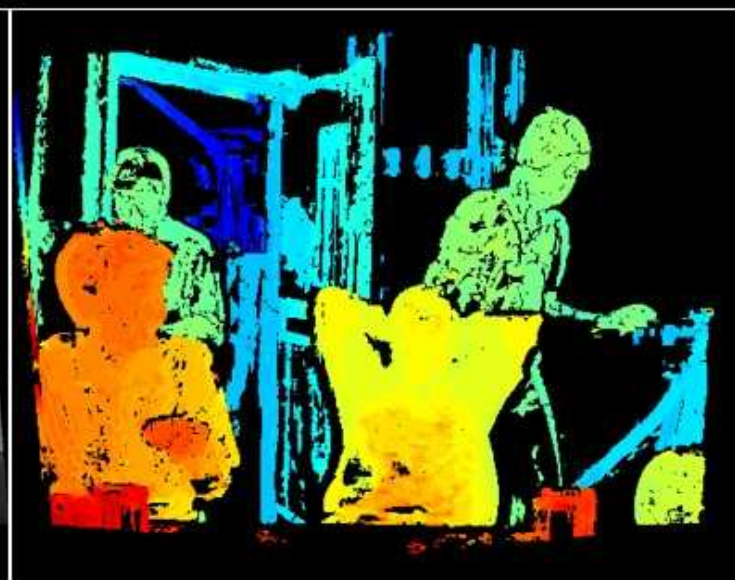
left image

disparity map

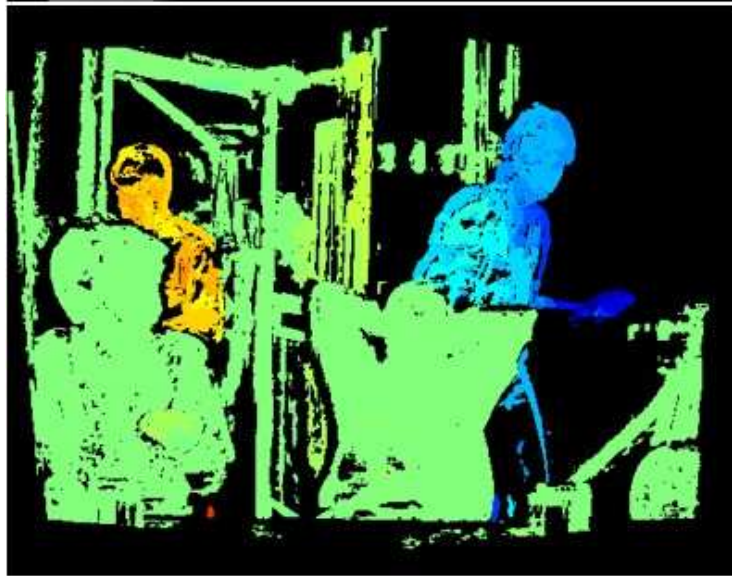
$I_L$



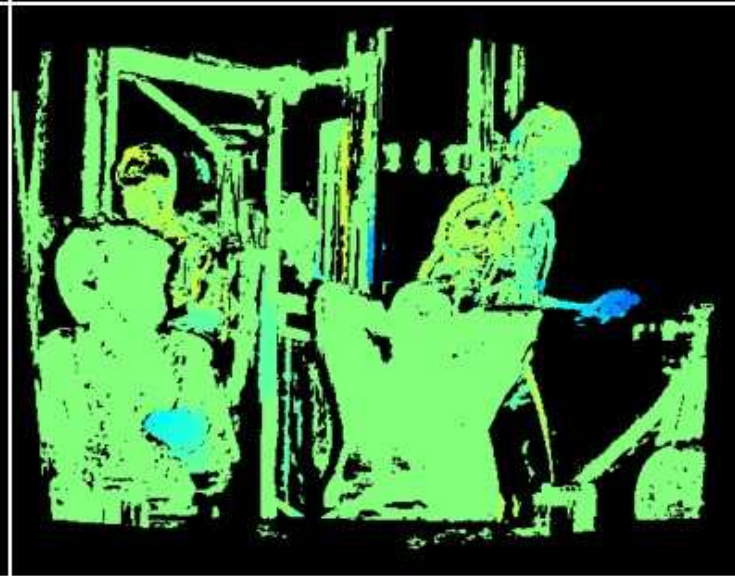
$D$



$F_x$



$F_y$



horizontal optical flow map

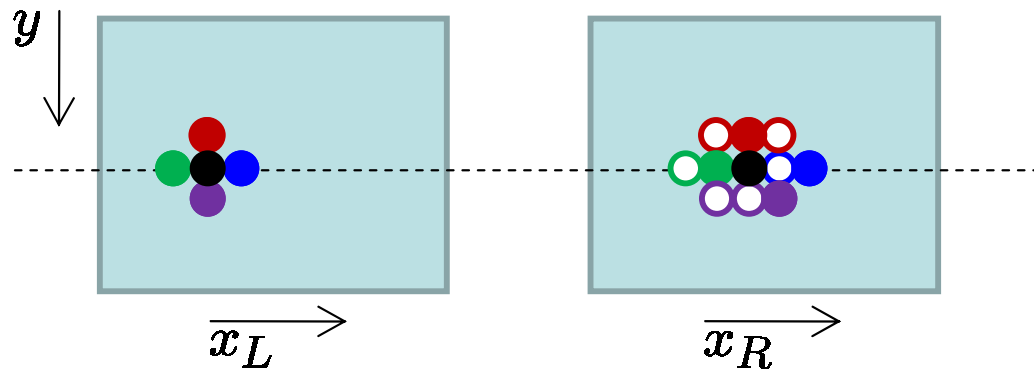
Vertical optical flow map

- Ambiguity of the correspondence problem – What helps?
  - Epipolar constraint
  - Spatial smoothness (but occlusions, object and motion boundaries)
    - Neighbouring pixels usually have similar disparities, optical flow
  - Temporal smoothness (but occlusions)
    - None of the disparity and optical flow maps change abruptly
  
- Explicit regularization – Global energy minimization
  - Often used in the literature  $\Rightarrow$  MRF, variational formulation
  - Computationally intensive
  - Artifacts caused by the prior model winning over the weak data
  
- Discriminability based
  - Finds unambiguous parts of the solution  $\Rightarrow$  semi-dense matching

- Basic Ideas:
  - Set of initial correspondences (seeds)
  - Other correspondences found in a neighbourhood of these seeds (points which are close have similar disparity and optical flow)
  - New correspondences found become new seeds
- Seed growing **stereo** algorithm [Cech-PAMI-2010]
  - Tradeoff between global energy methods and greedy local methods, the growing process constraints possible solution
  - Robust against wrong seeds
  - Very fast (search space reduction),  $\mathcal{O}(n^3) \rightarrow \mathcal{O}(n^2)$
  - Semi-dense (not fully dense), but identifies ambiguous (textureless) regions

# Correspondence growing in Stereo

- Stereo (2 still images only)
- a correspondence seed:  $s = (x_L, x_R, y)$



$$p^* = \arg \max_{p \in \mathcal{N}(s)} \text{corr}(p)$$

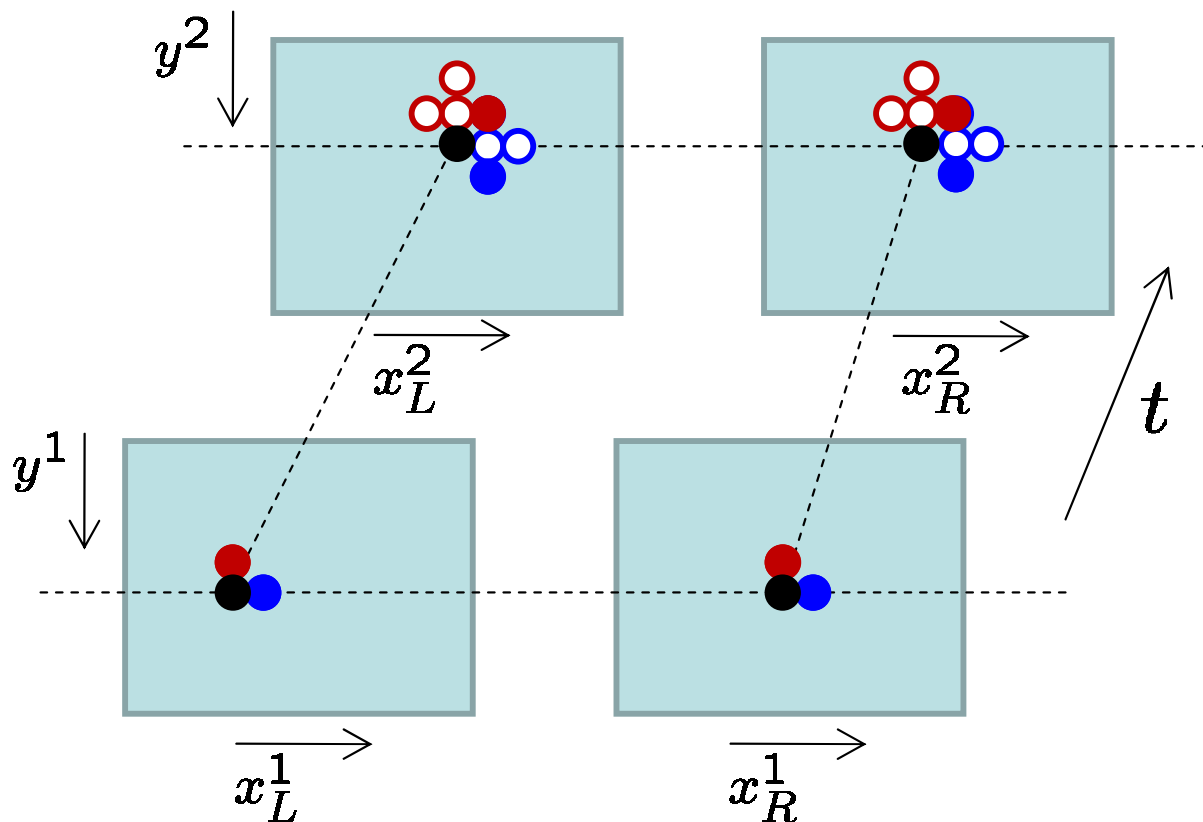
If  $\text{corr}(p^*) > \tau$ ,  
accept a new match.





# Growing the Scene Flow

- Growing disparity + optical flow at once
- Correspondence seed:  $s = (x_L^1, x_R^1, y^1, x_L^2, x_R^2, y^2)$
- disparity map for  $t = 1$  is given
- seeds obtained by matching Harris points + LK tracker
- similarity:  $\text{corr}(p) = \frac{1}{3}(c_{LR}^{22} + c_L^{12} + c_R^{12})$



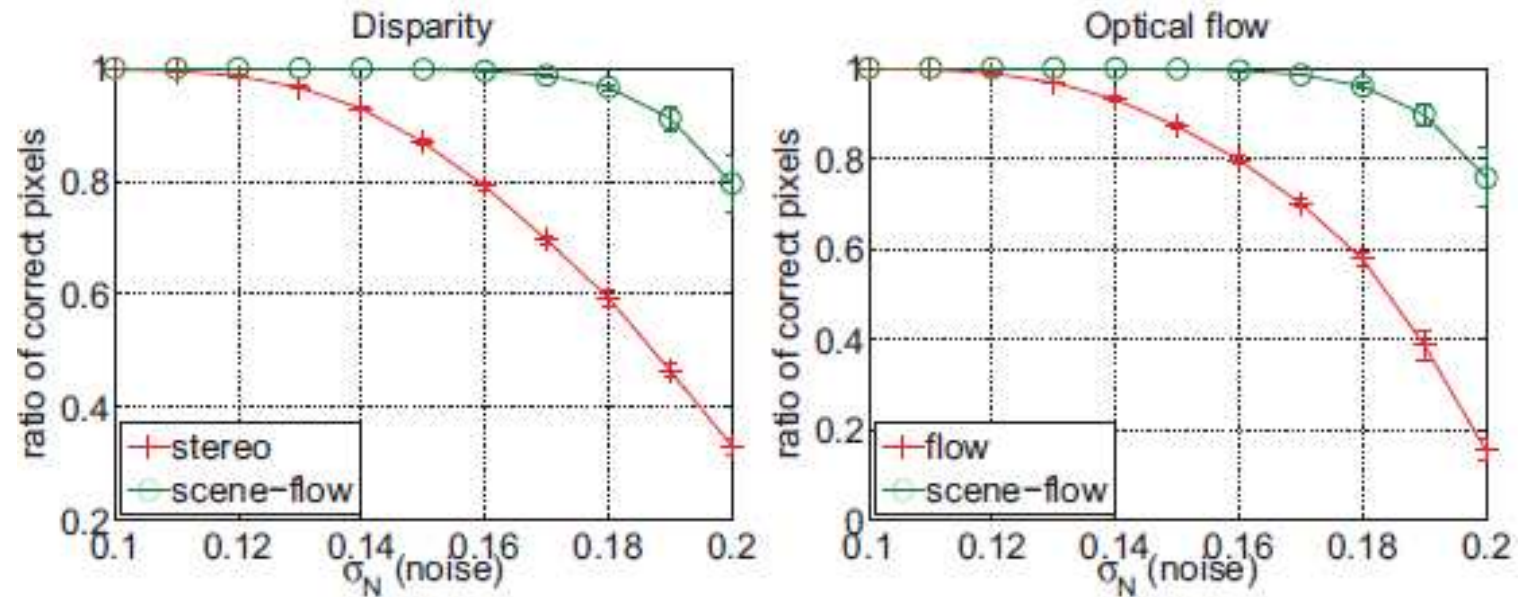
$$p^* = \arg \max_{p \in \mathcal{N}(s)} \text{corr}(p)$$

If  $\text{corr}(p^*) > \tau$ ,  
accept a new match.

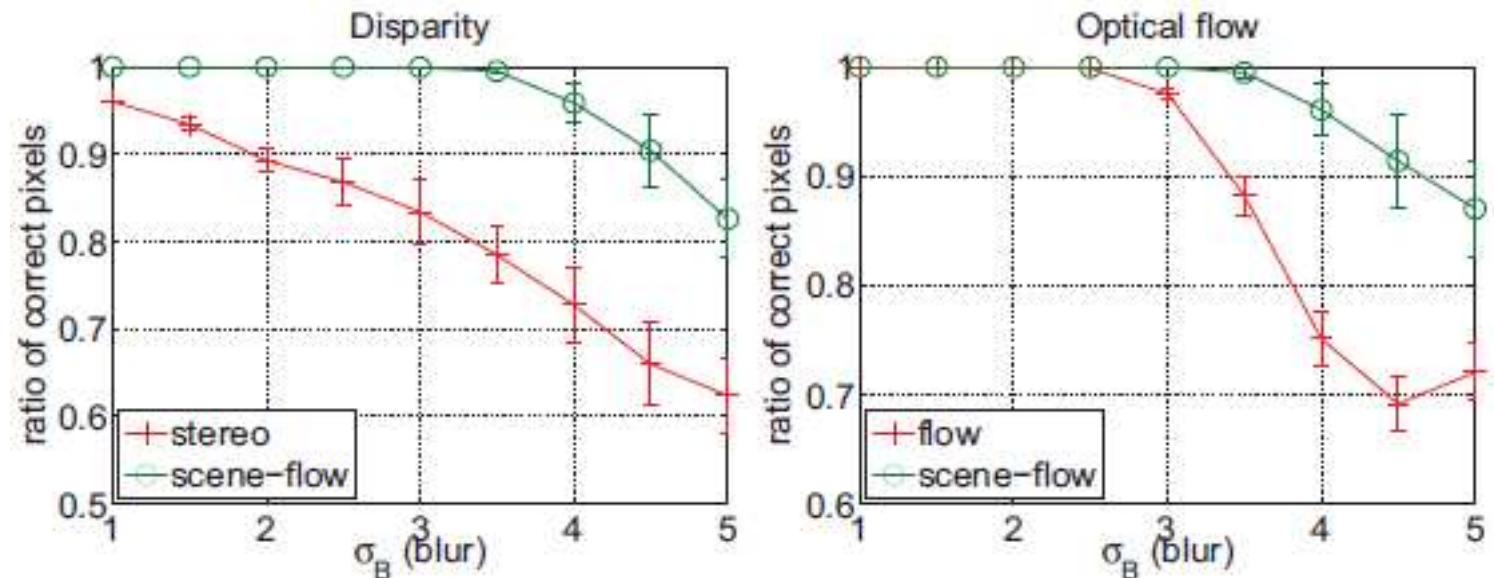
# Results: Synthetic ground-truth experiment

- Synthetic stereo sequence (textured plane moving)

(1) noise



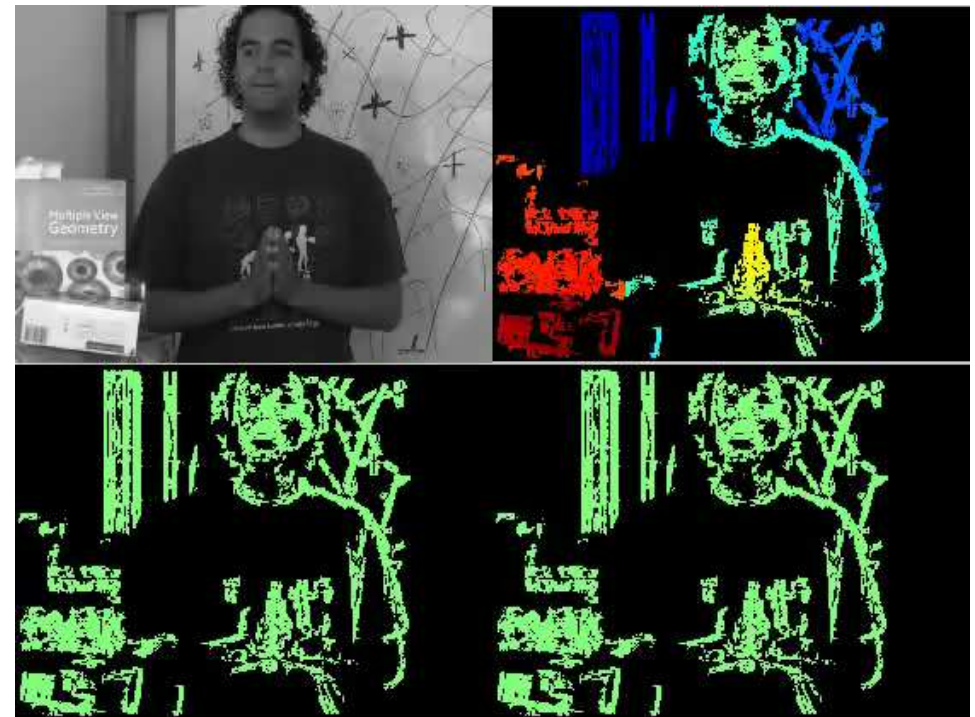
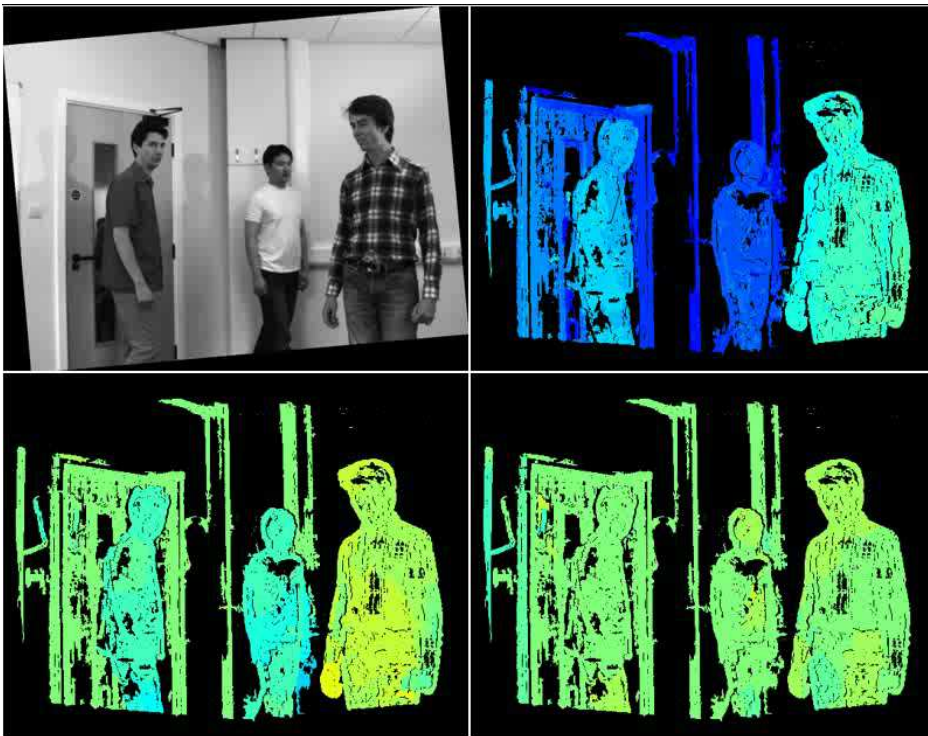
(2) blur



- Joint disparity and optical flow better performance than independently

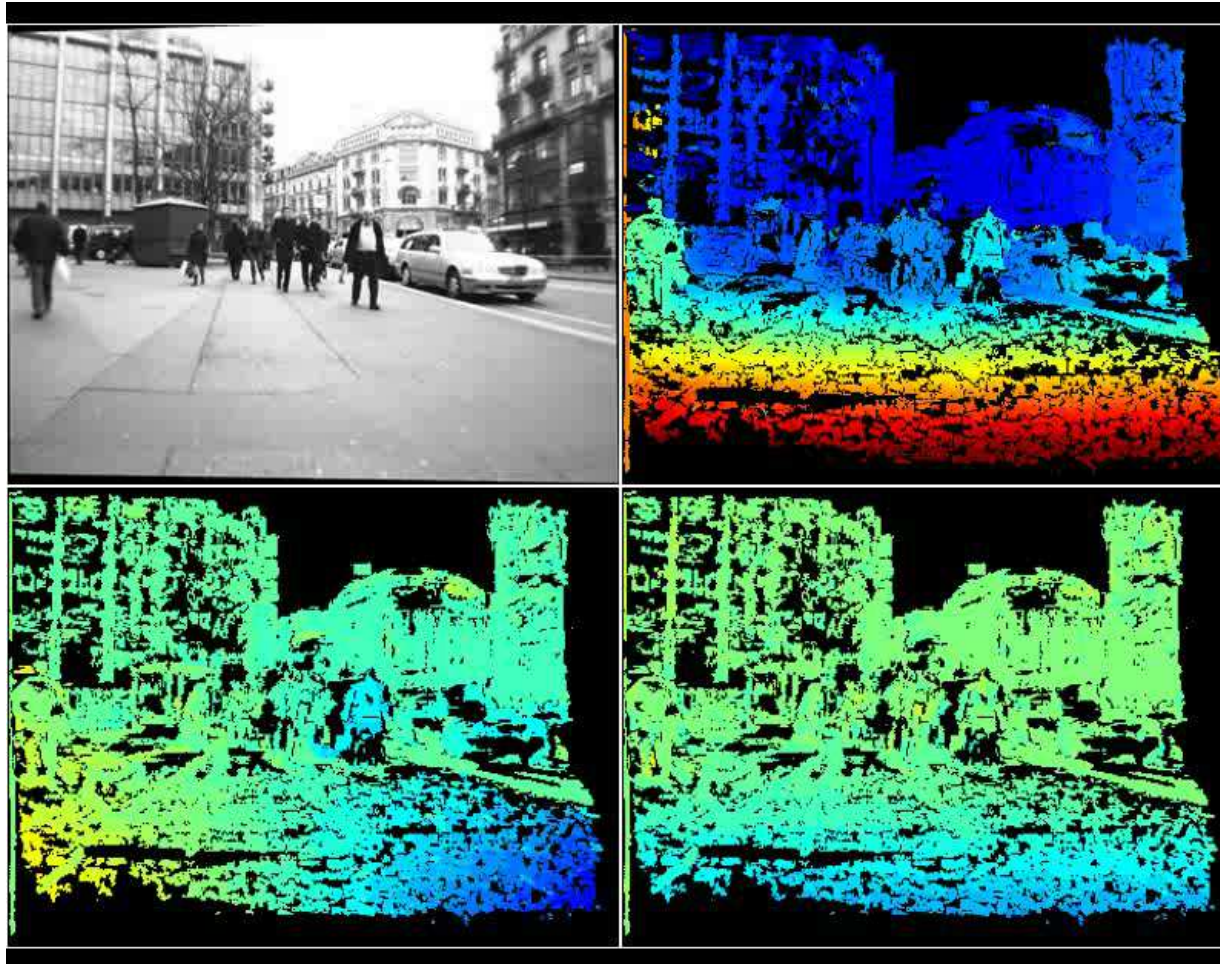
# Results: Real data (1)

- Static camera
  - INRIA dataset



## Results: Real data (2)

- Moving camera
  - pedestrian dataset by ETH Zurich



- Allows large displacement between frames (>30 pixels)
- Occlusion boundaries well preserved, no smoothing artifacts
- Disparity maps are temporally coherent (better results than frame by frame stereo)
- Optical flow maps are more precise than in a single camera setup
- Fast (VGA image in ~ 1.5 s), not a significant extra cost w.r.t. the stereo
  - Low algorithmic complexity due to search space reduction:  
$$\mathcal{O}(n^5) \rightarrow \mathcal{O}(n^2)$$
- Results are not fully dense, but semi-dense only
- Extended version of this algorithm in CVPR 2011
  - Algorithm incorporated in the pipeline for processing a stereo sequence with motion prediction
  - Experimental comparison with State-of-the-art methods of scene-flow, spatiotemporal stereo, and optical flow

