



# INTRA-FRAME PREDICTION WITH LAPPED TRANSFORMS FOR IMAGE CODING

**Rafael Galvão de Oliveira**

**Beatrice Pesquet**





# Overview

- Motivation
- Lapped transforms: background
- Intra-frame prediction
  - Difficulties for LT
  - Proposed Solution
  - Modification in the mode selection
- Experimental Results
- Conclusion and future work



# Motivation: Lapped transforms in image coding

- Reduction of blocking effects
- Exploitation of redundancies among neighboring blocks
- Superior performance for encoding
  - Objectively and subjectively
  - Higher complexity
- JPEG XR

[1] de Oliveira, R.G.; de Queiroz, R.L.; , "Intra prediction versus wavelets and lapped transforms in an H.264/AVC coder," *Image Processing, 2008. ICIP 2008. 15th IEEE International Conference on* , vol., no., pp.137-140, 12-15 Oct. 2008



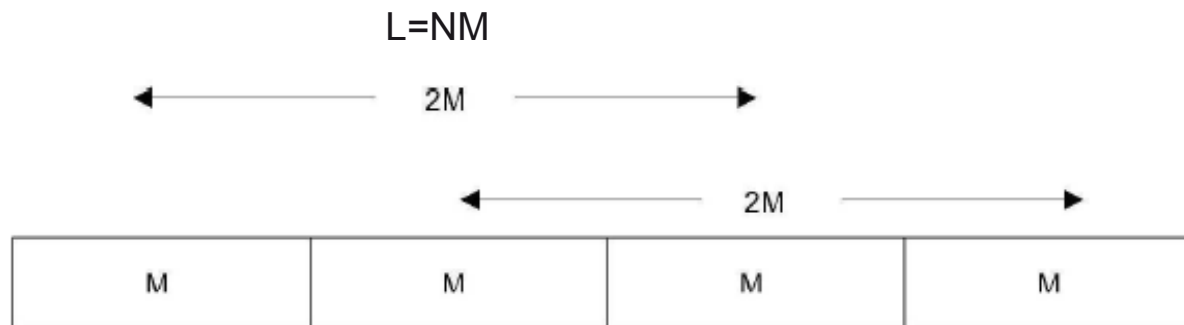
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# Lapped Transforms: background

- Differently from block transforms, lapped transforms have a bigger support than the traditional block



$$\mathbf{v}_m^T = \left[ x \left( mM - (N-1) \frac{M}{2} \right) \cdots x \left( mM - (N+1) \frac{M}{2} - 1 \right) \right]$$



# Lapped Transforms: background

## ■ Direct Transform

$$Y_m = P \cdot v_m$$

$$P = [P_0 P_1 \dots P_{N-1}]$$

$$Q = [Q_0 Q_1 \dots Q_{N-1}]$$

## ■ Inverse Transform

$$\hat{v}_m = Q^T \cdot Y_m$$

$$\hat{v}_m \neq v_m$$

$$Q^T \cdot P \neq I$$

## ■ Perfect reconstruction

$$\sum_{k=0}^{N-1-m} Q_k^T P_{k+m} = \sum_{k=0}^{N-1-m} Q_{k+m}^T P_k = \delta(m) I_M$$



# Lapped Transforms: reconstruction

- **The blocks cannot be reconstructed independently**
- **The signal is reconstructed accumulating the contribution of several neighboring blocks**
- **Border treatment has to be carried out**



# Overview

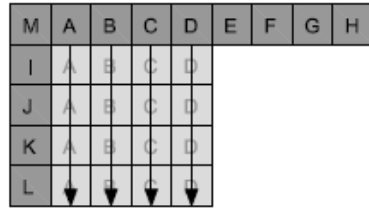
- Motivation
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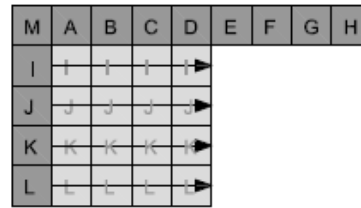


# Intra-frame prediction in H.264/AVC

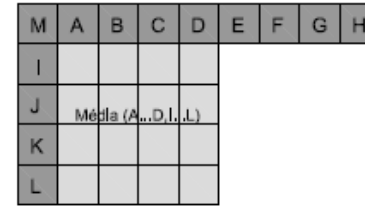
4x4 and  
8x8 blocks



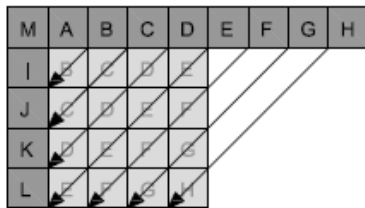
Mode 0



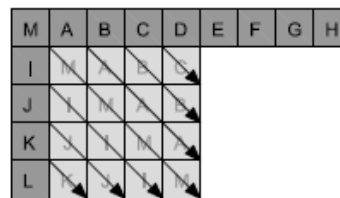
Mode 1



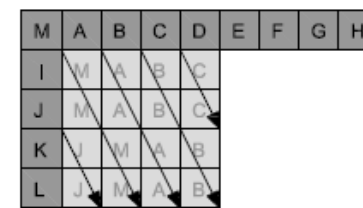
Mode 2



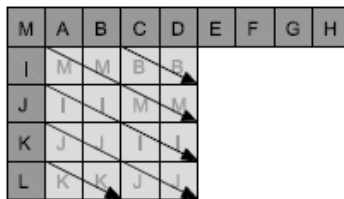
Mode 3



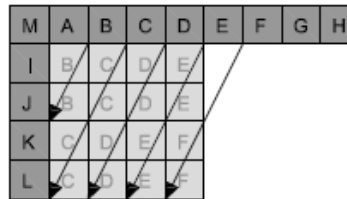
Mode 4



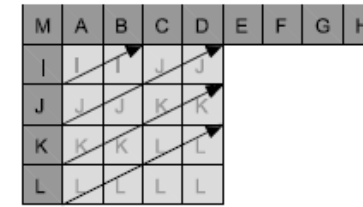
Mode 5



Mode 6



Mode 7



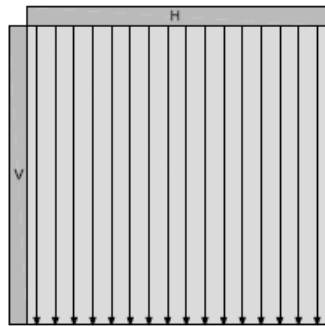
Mode 8

[2] de Queiroz, R.L.; Ortis, R.S.; Zaghetto, A.; Fonseca, T.A.; , "Fringe benefits of the H.264/AVC,"  
*Telecommunications Symposium, 2006 International* , vol., no., pp.166-170, 3-6 Sept. 2006

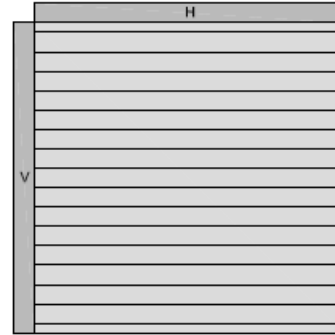


# Intra-frame prediction in H.264/AVC

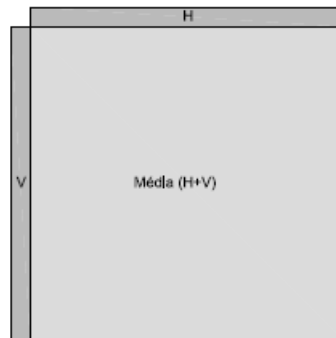
16x16 blocks



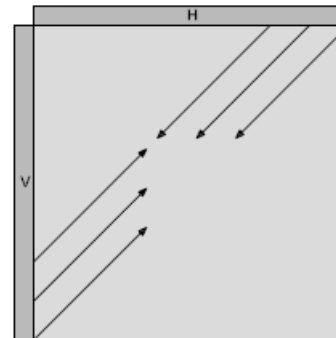
Mode 0



Mode 1

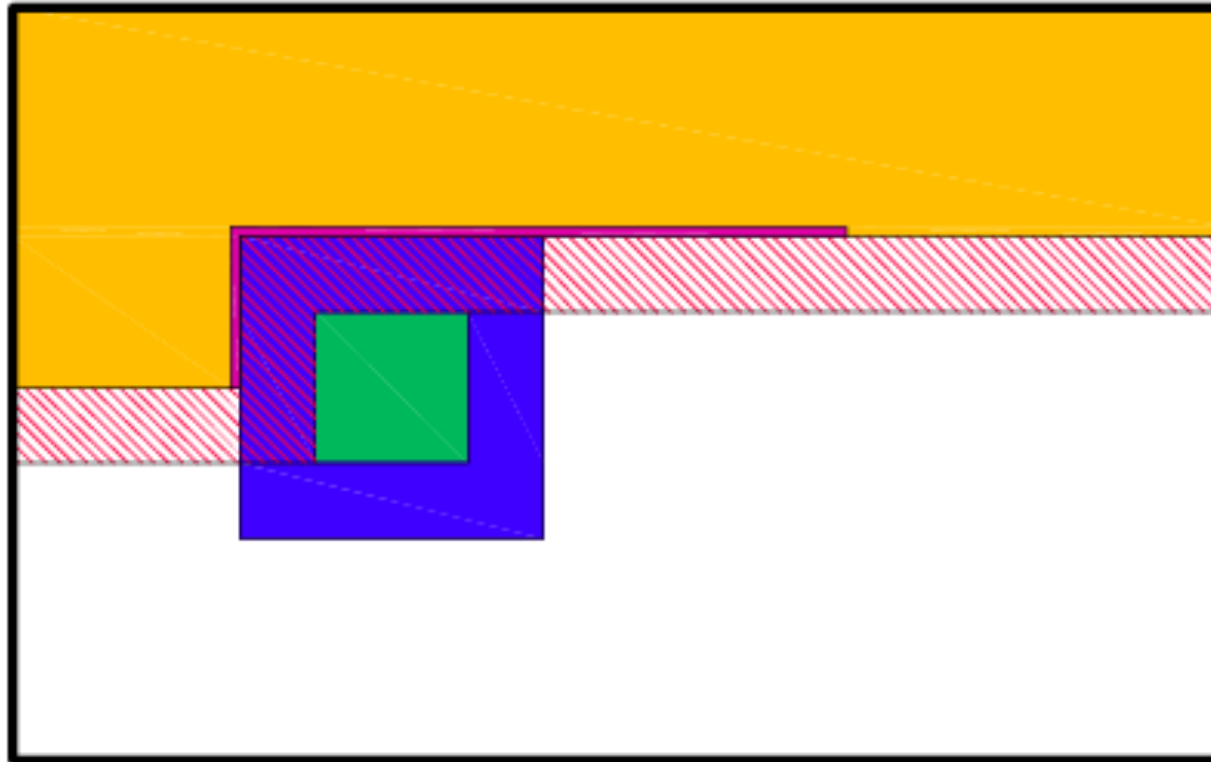


Mode 2



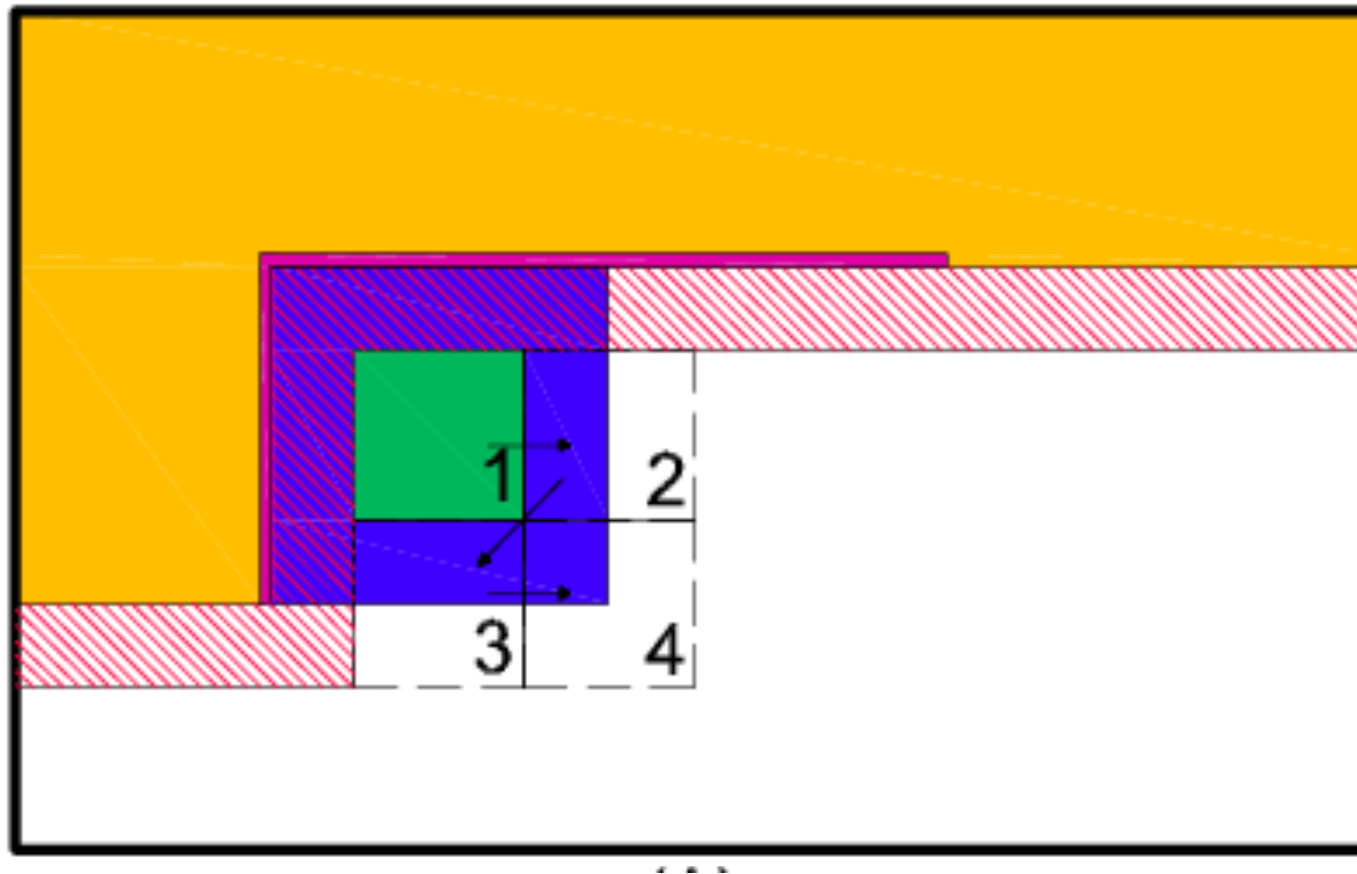
Mode 3

# Intra frame prediction and Lapped Transforms

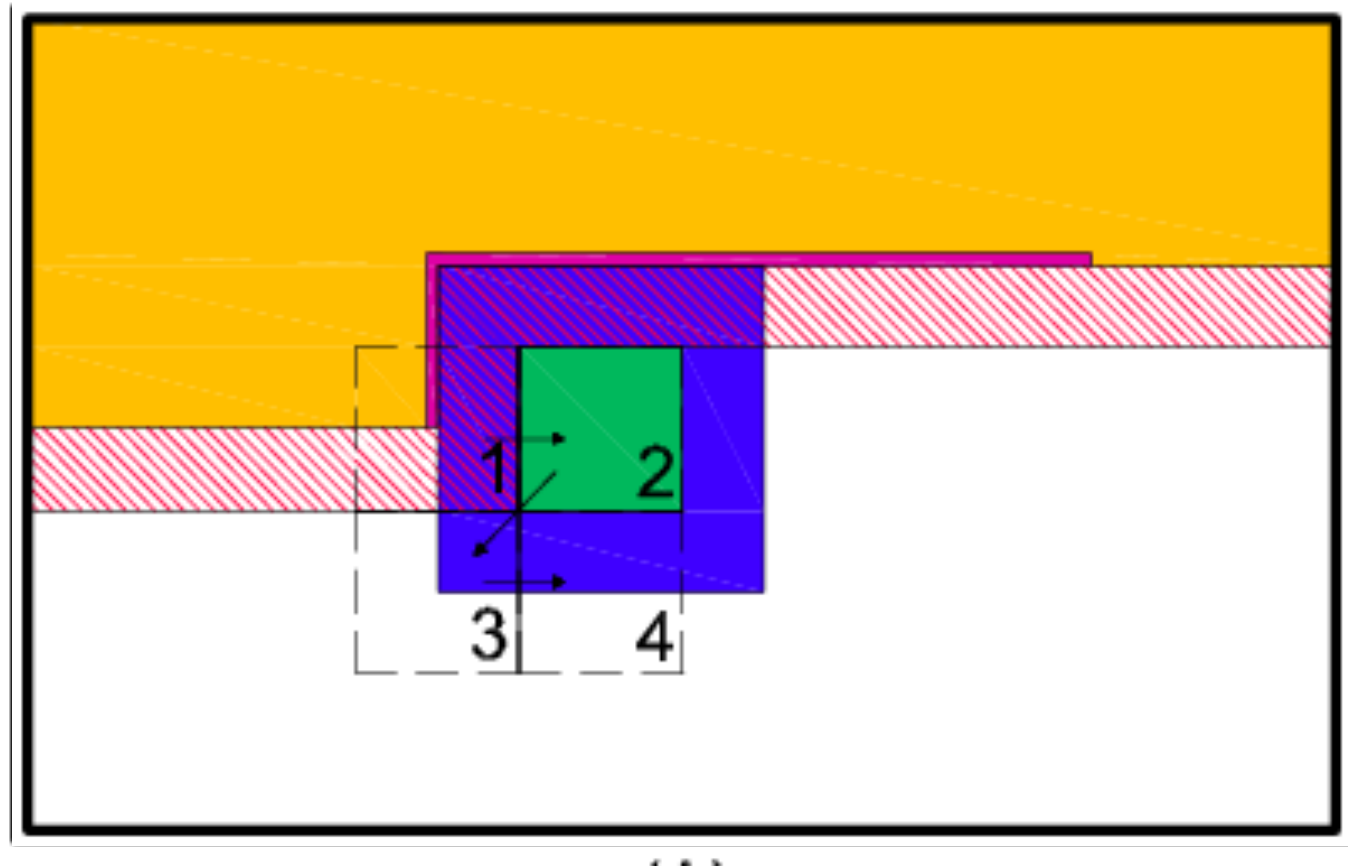


- Block Extension
- Region with reconstructible pixels
- Block to be encoded
- Region with pixels not yet reconstructable
- Pixels used in the prediction

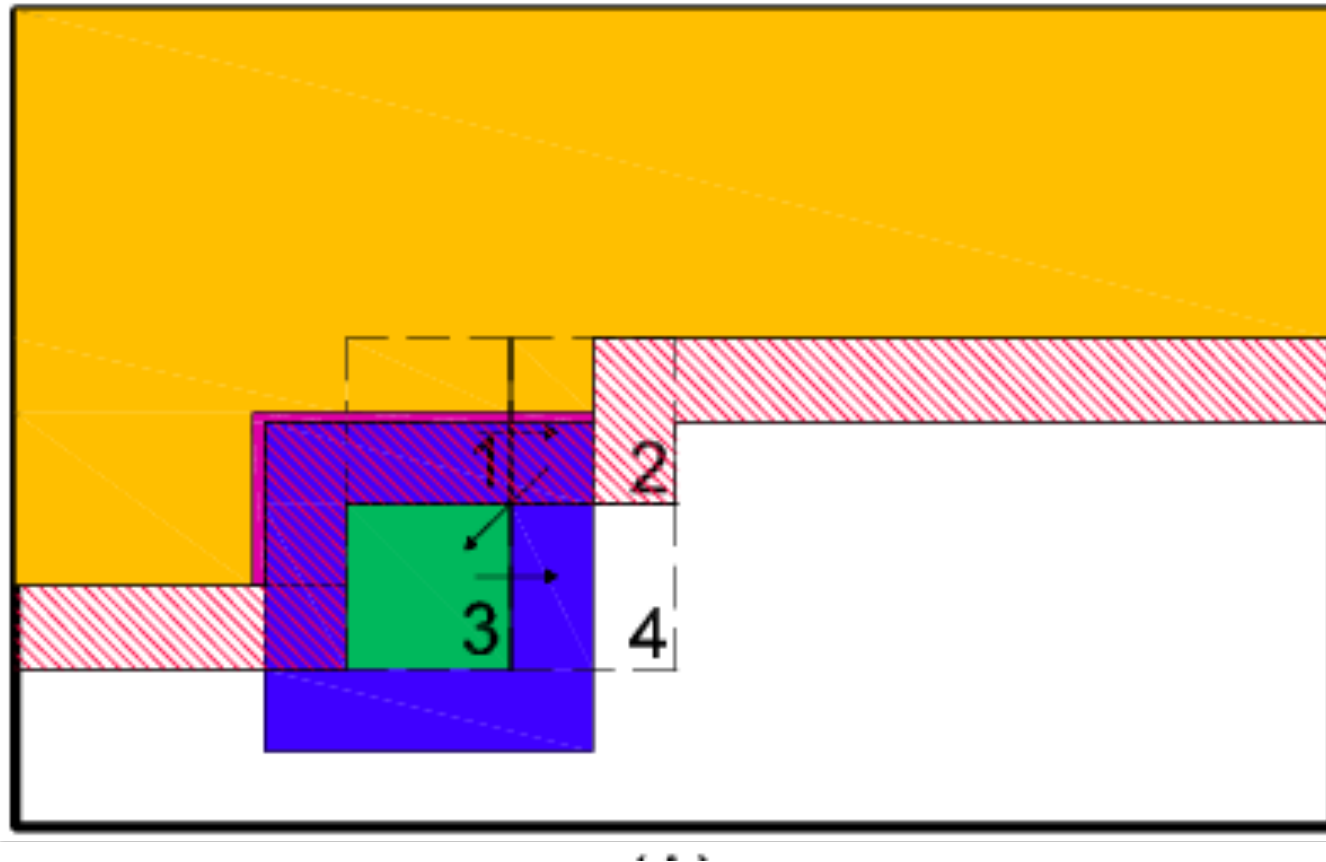
# Intra frame prediction and Lapped Transforms



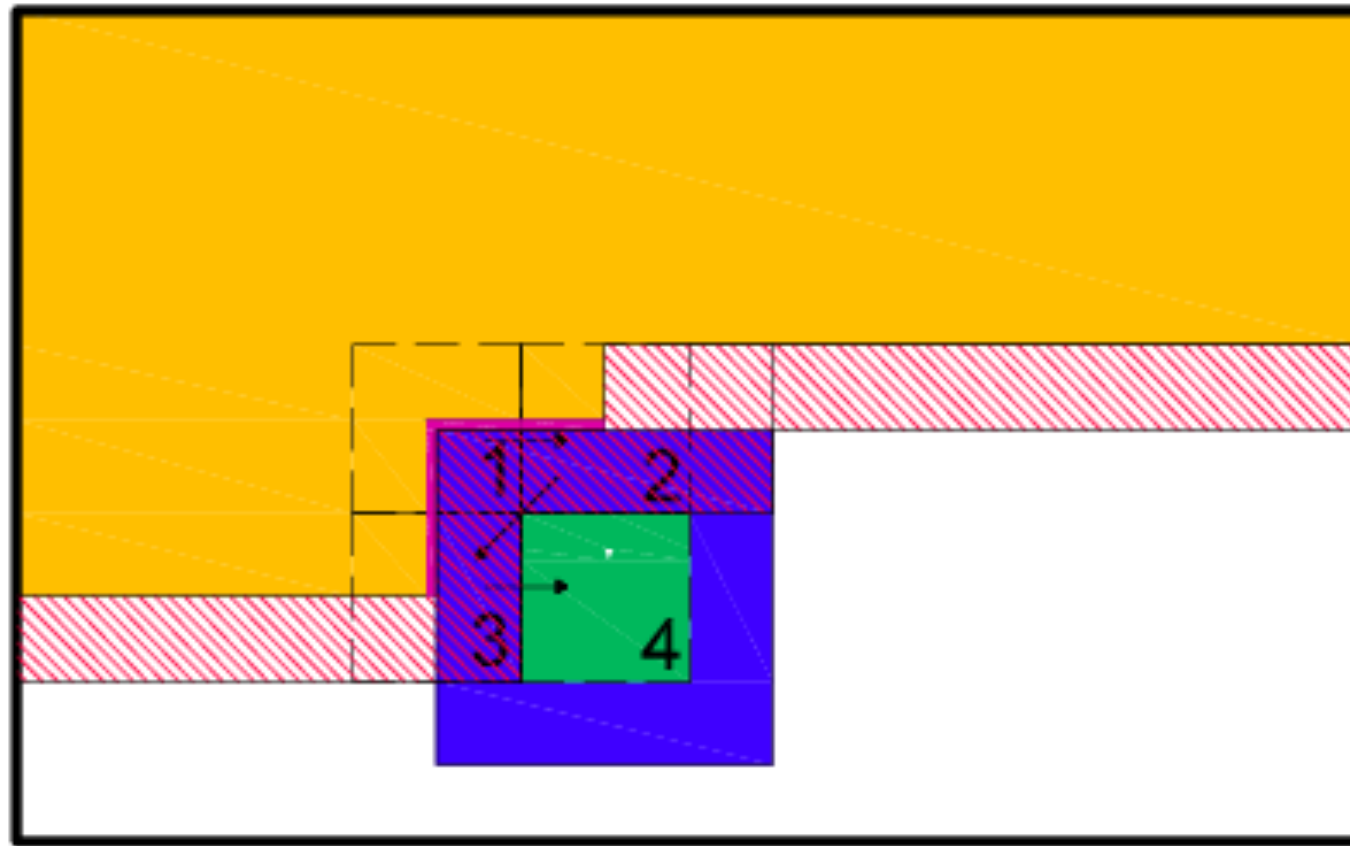
# Intra frame prediction and Lapped Transforms



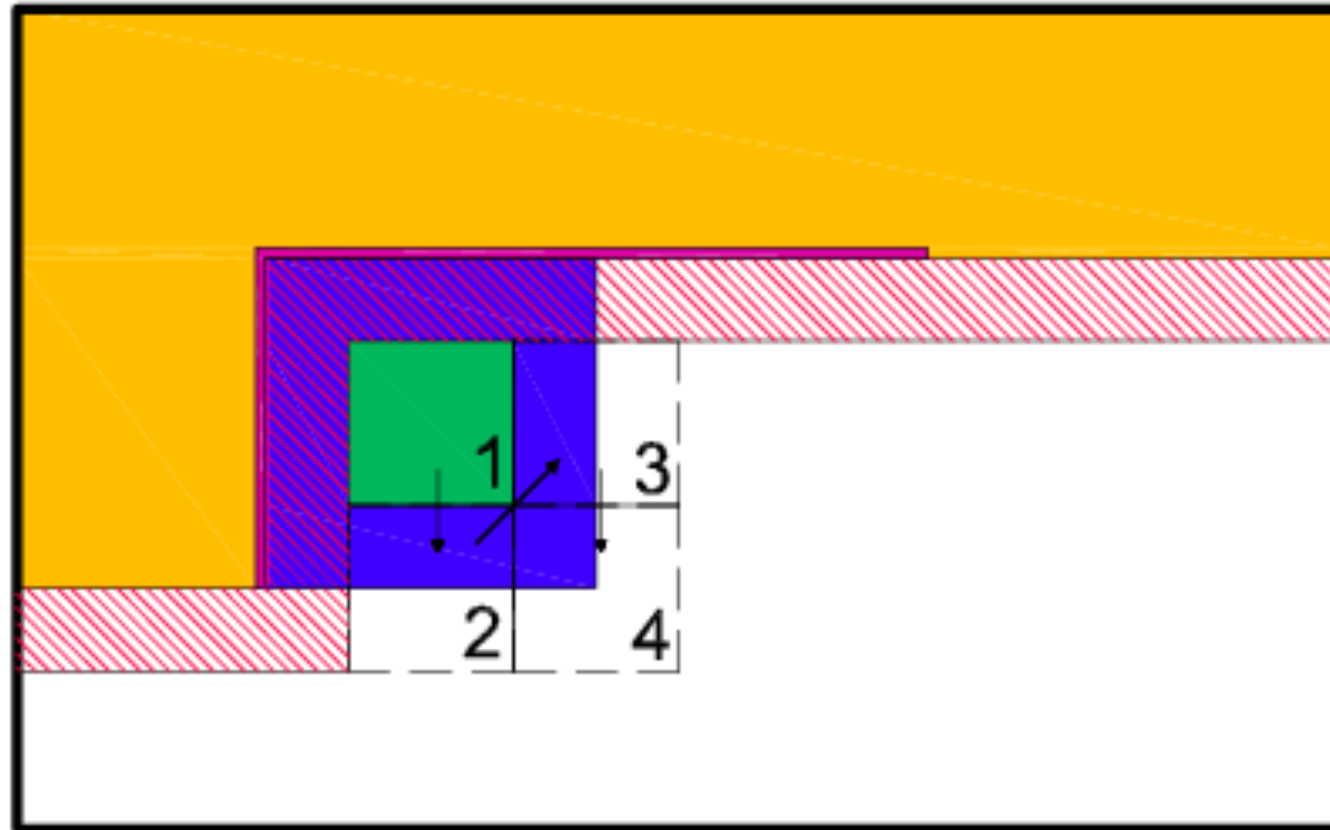
# Intra frame prediction and Lapped Transforms



# Intra frame prediction and Lapped Transforms

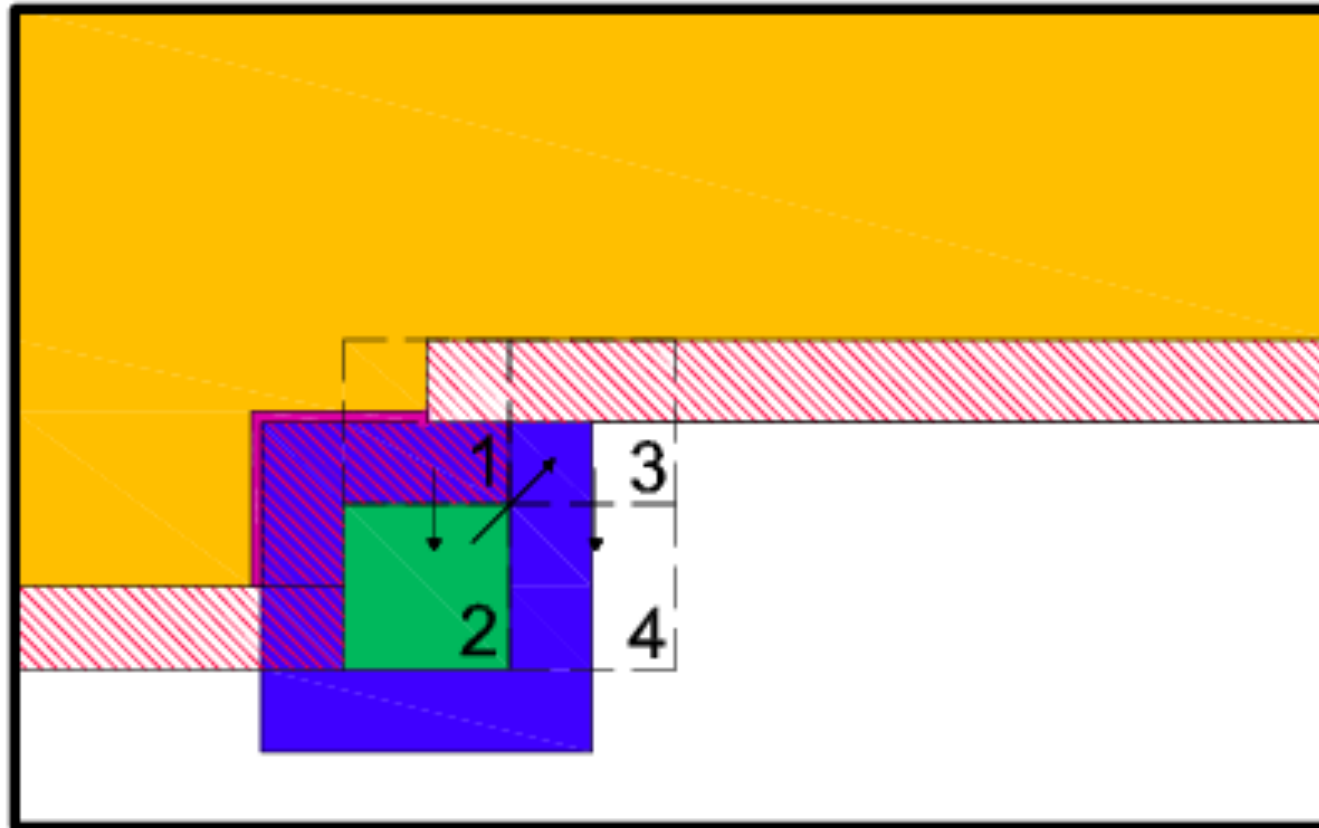


# Intra frame prediction and Lapped Transforms

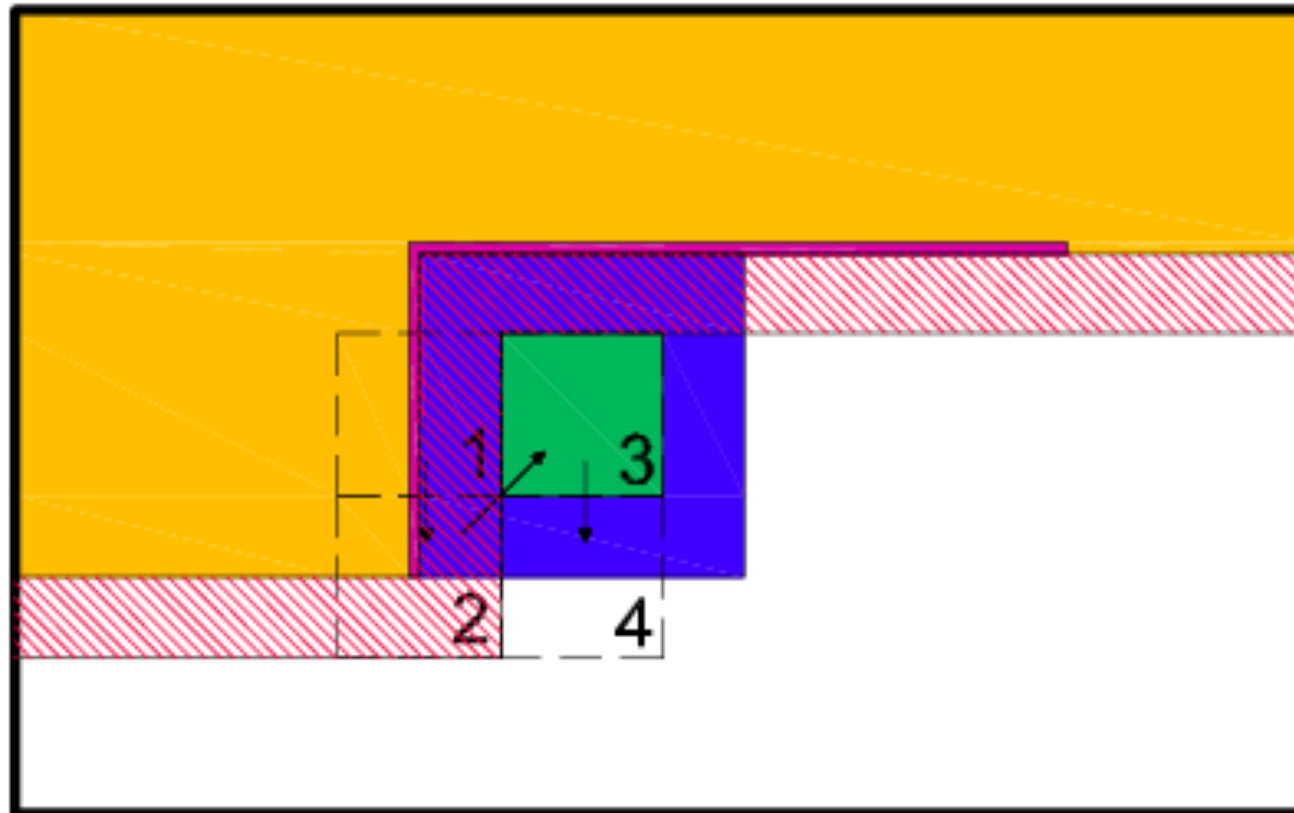




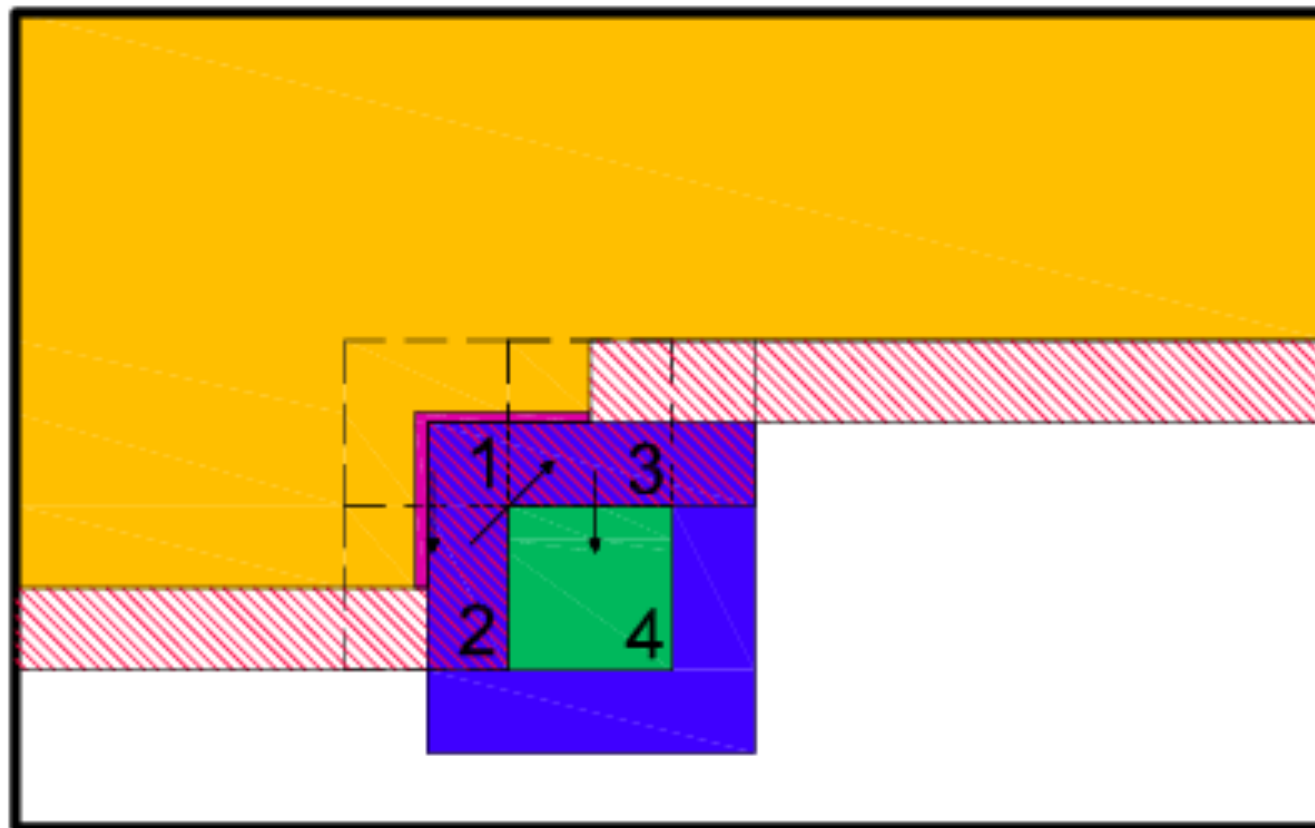
# Intra frame prediction and Lapped Transforms



# Intra frame prediction and Lapped Transforms



# Intra frame prediction and Lapped Transforms



# Intra frame prediction and Lapped Transforms: analysis/reconstruction

## ■ Prediction, transform and reconstruction

Prediction  $\mathbf{R}_{mn} = \mathbf{V}_{mn} - \text{Pred}_{mn}$

Direct transform  $\mathbf{Y}_{mn} = \mathbf{P} \cdot \mathbf{R}_{mn} \cdot \mathbf{P}^T$

Inverse LT  $\widehat{\mathbf{R}}_{mn} = \mathbf{Q}^T \cdot \mathbf{Y}_{mn} \cdot \mathbf{Q}$

$$\widehat{\mathbf{V}}_{mn} = \widehat{\mathbf{R}}_{mn} + \mathbf{Q}^T \cdot \mathbf{P} \cdot \text{Pred}_{mn} \cdot \mathbf{P}^T \cdot \mathbf{Q}$$



# Mode Selection

## ■ SAD

$$SAD = \sum_{i=0}^{M-1} \sum_{j=0}^{M-1} |x_{nm}(i, j) - \text{Pred}_{nm}(i, j)|$$

## ■ WSAD

$$WSAD = \sum_{i=0}^{L-1} \sum_{j=0}^{L-1} \left| W_{ij} \left( v_{nm}(i, j) - \text{Pred}_{nm}(i, j) \right) \right|$$

Weighting matrix  $W = Q^T \cdot P \cdot \text{Ones} \cdot P^T \cdot Q$

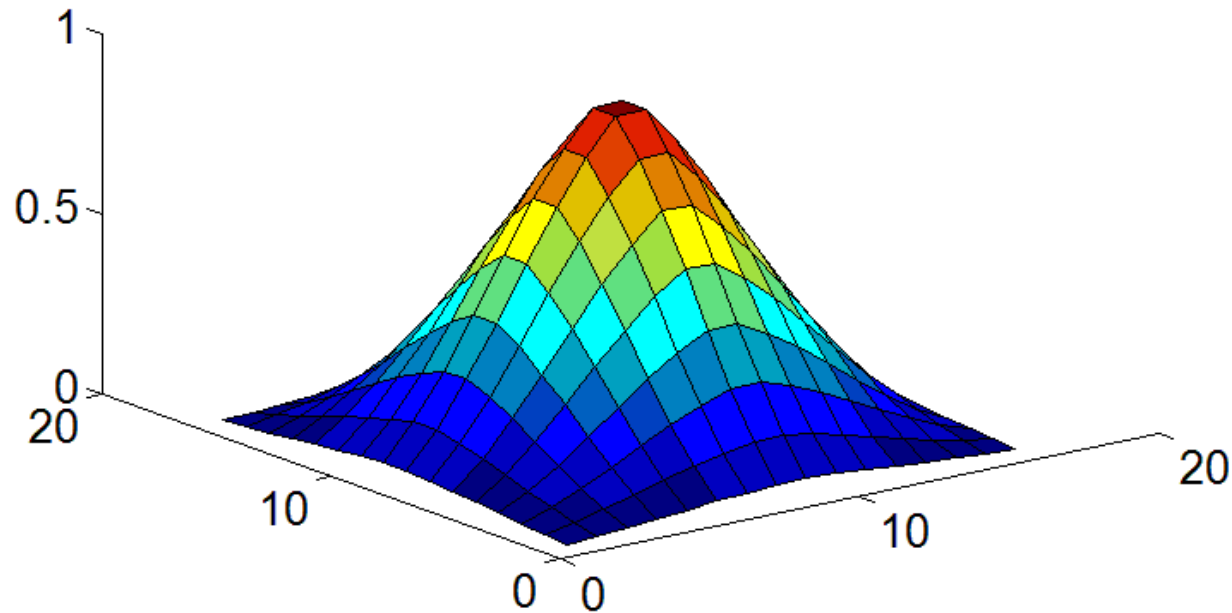
## ■ RDO

- spatial reconstruction not fully available
- distortion measure in the transform domain
- $e_{ij}$  is the energy of the synthesis filter

$$D = \sum_{ij} e_{ij} \left( Y_{ij} - Y'_{ij} \right)^2$$



## Weighting Window: example



- GLBT 8x16
- P,Q optimized for maximizing the coding gain of an AR(1) model with  $\rho=0.95$



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## Experimental results

- **Implementation has been carried in a JPEG coder**
- **The coding block fixed to 8x8 pixels**
- **Lapped transform used in the tests: GLBT 8x16**
  - Overlap of 2: more blocks benefit from the prediction
  - GLBT: best performance for this overlapping factor
  - Overlapping of 2: prediction block 16x16
  - Only four modes available for the prediction using LT





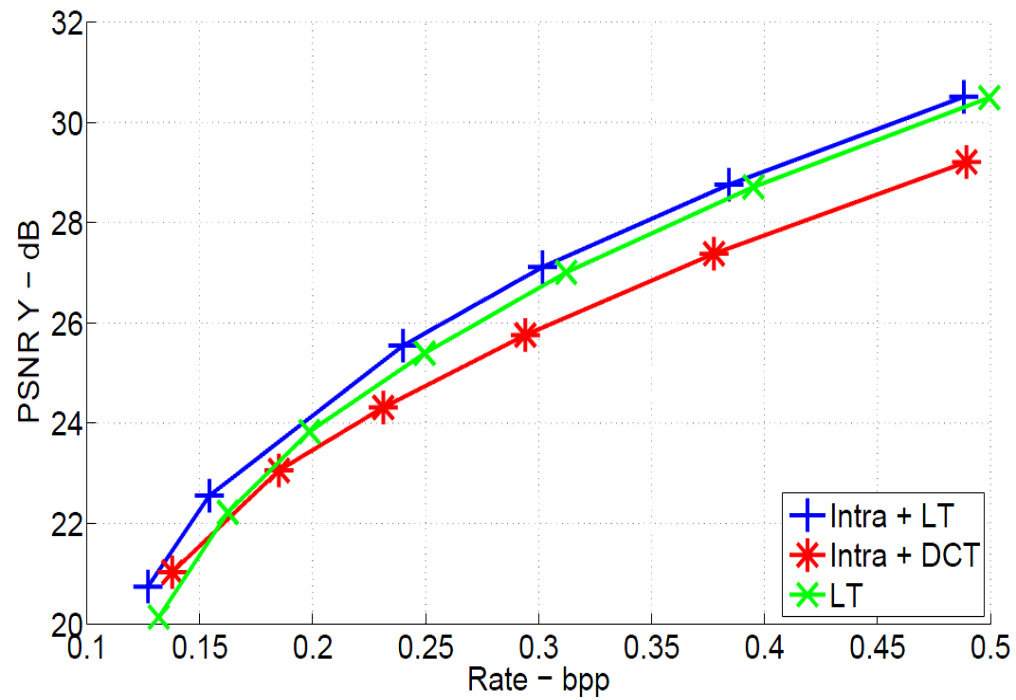
## Implementation Details

- **For comparison reasons, the traditional intra frame prediction was also implemented in JPEG and the modes of the traditional scheme were encoded in the same way as proposed in H.264/AVC**
- **Modes of the proposed scheme encoded using 2 bits**
  - Using the mode prediction represented a rate increase (not both neighbors available for the prediction)
- **The direct application (no prediction) of lapped transforms also tested**



# RD Results (1)

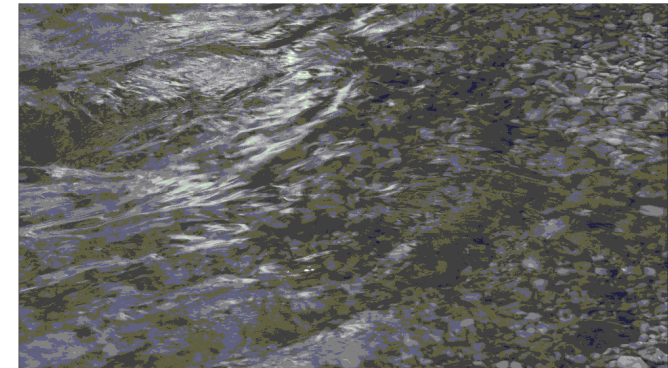
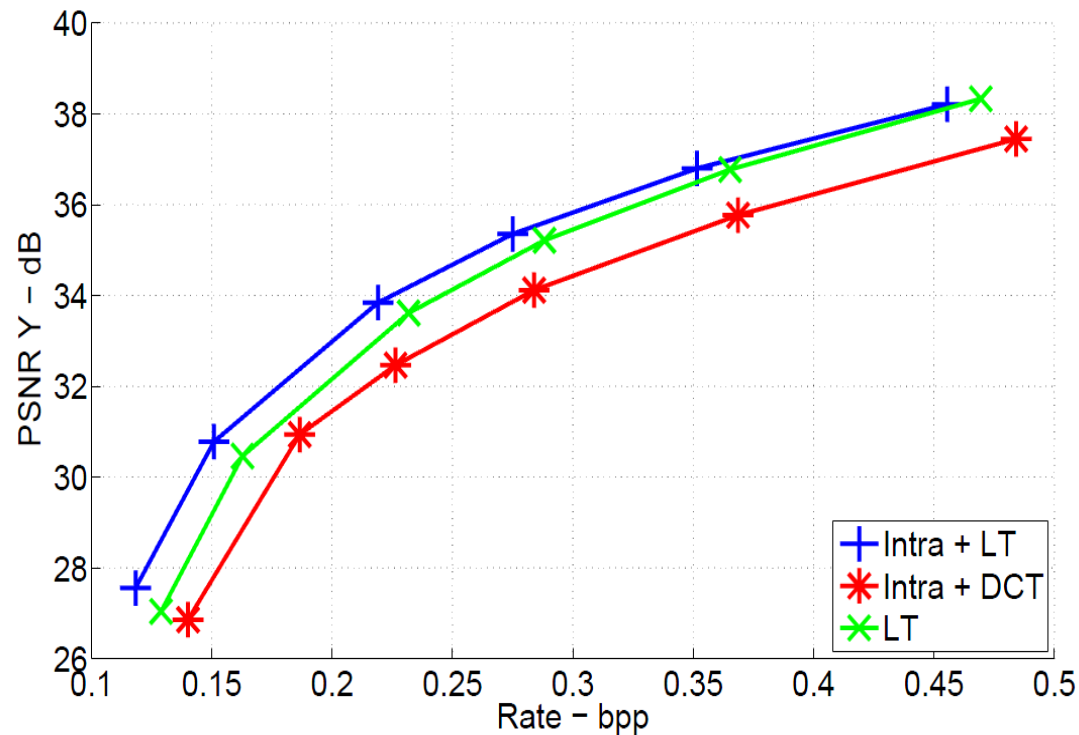
## ■ Barbara (512x512)





## RD Results (2)

### ■ Riverbed (1920x1080) – first frame





## Results: Bjontegaard metric (low bitrate)

Image (resolution)	G1(dB)	% R1	G2(dB)	% R2
Barbara (512 × 512)	0.79	-11.21	0.31	-3.98
Goldhill (512 × 512)	0.51	-8.16	0.32	-4.57
Lena (512 × 512)	0.40	-4.07	0.35	-3.90
Riverbed (1080p)	1.12	-14.64	0.90	-4.72
Sunflower (1080p)	1.95	-7.65	1.48	-7.02

1. Comparison between the proposed scheme and Intra-prediction with DCT
2. Comparison between the proposed scheme and the direct application of lapped transforms



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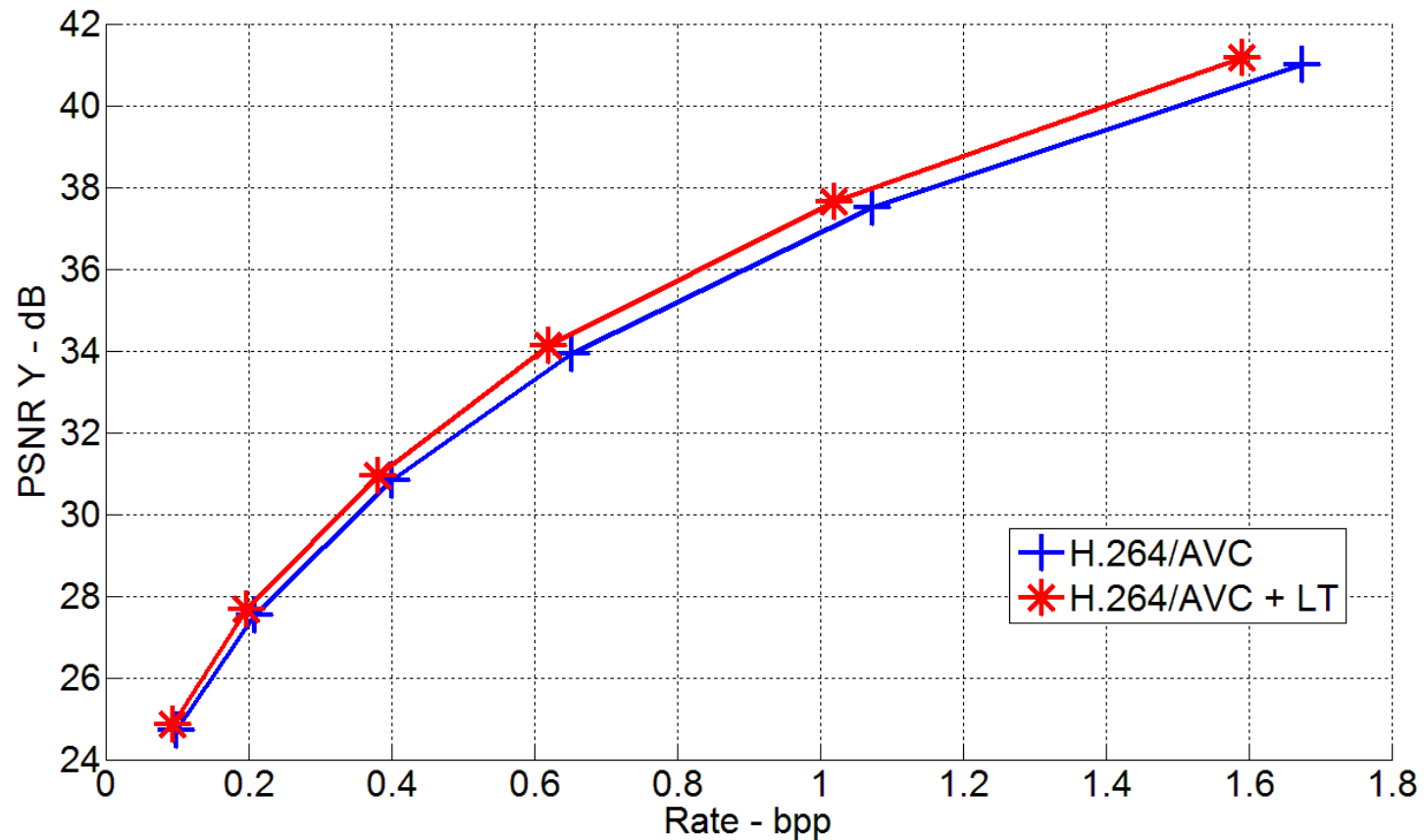


## Conclusion

- **The results show that intra-frame prediction can be adapted to be compatible with lapped transforms**
- **The proposed scheme outperforms the direct application of lapped transforms and the traditional intra prediction with DCT in all tested images**
- **For the moment, fewer prediction modes were implemented for 16x16 pixel blocks**



## Work in progress: RD Results(Barbara)





## Work in progress

- **Implementation in H.264/AVC available for the same conditions**
  - Competition with all the prediction modes
  - CABAC adapted to the integer DCT
  
- **Future work**
  - Variable size prediction blocks
  - Test other transforms (with other overlapping factors)
  - A extension to video of this work has been accepted in ICIP2011





# Thank you!