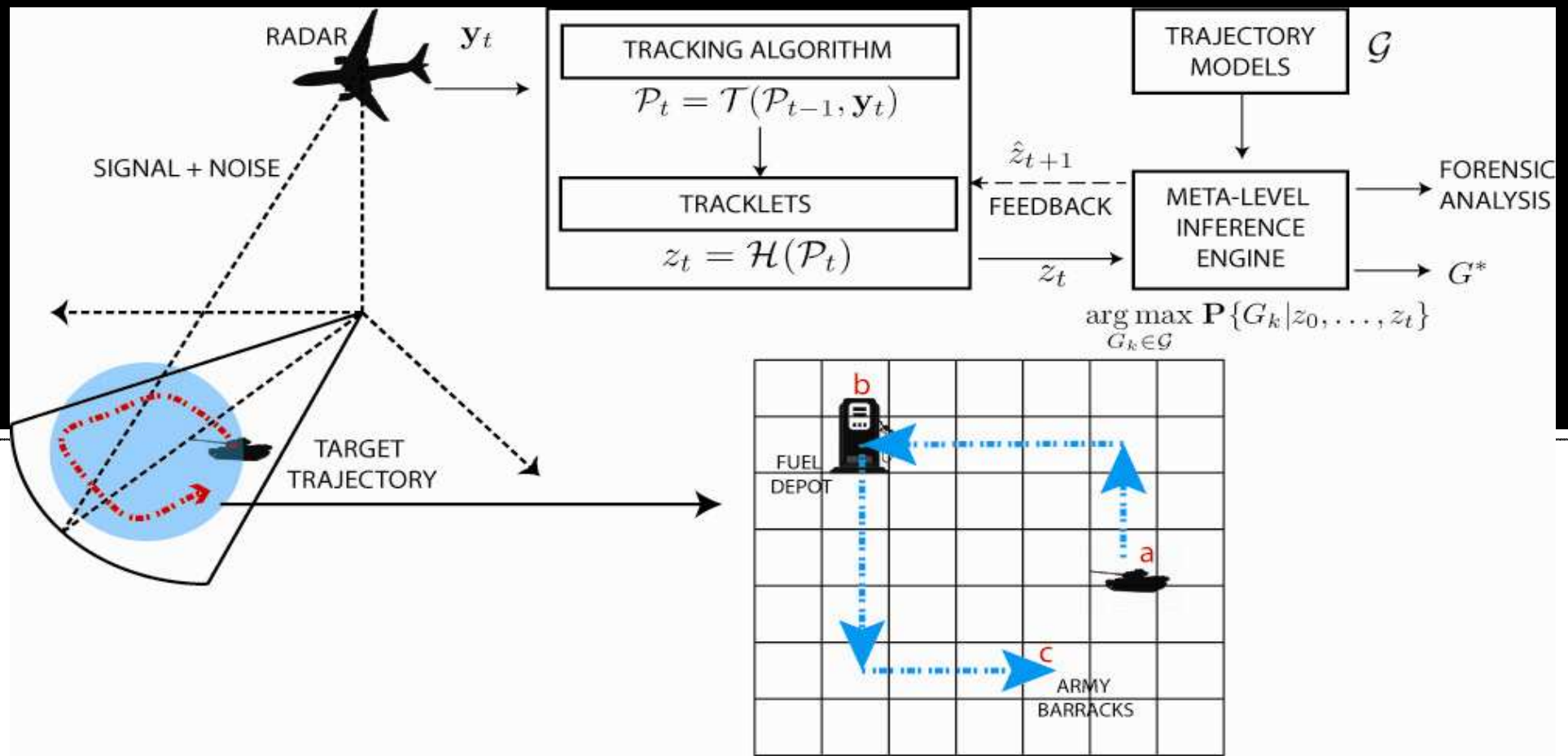


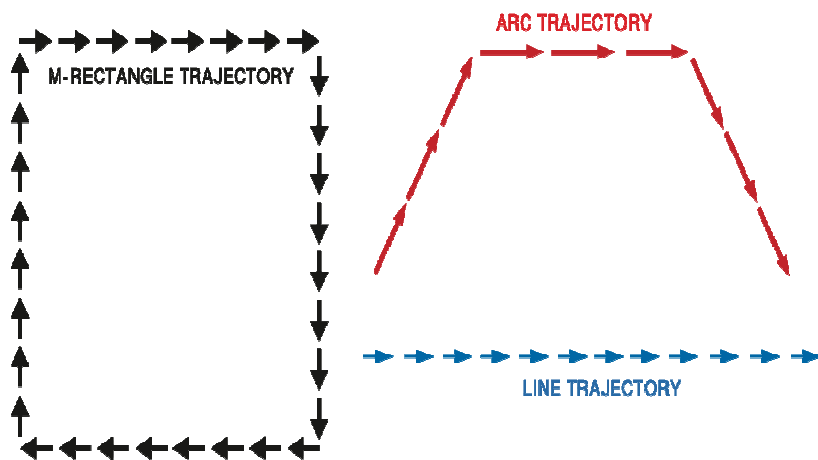
Vikram Krishnamurthy, University of British Columbia, Canada  
Coauthors: Mustafa Fanaswalla (UBC) and Langford White (U Adelaide)

# Destination Aware Target Tracking via Syntactic Signal Processing



# Syntactic patterns for Intent Inference

## Ex1: Abnormal Pattern of Life

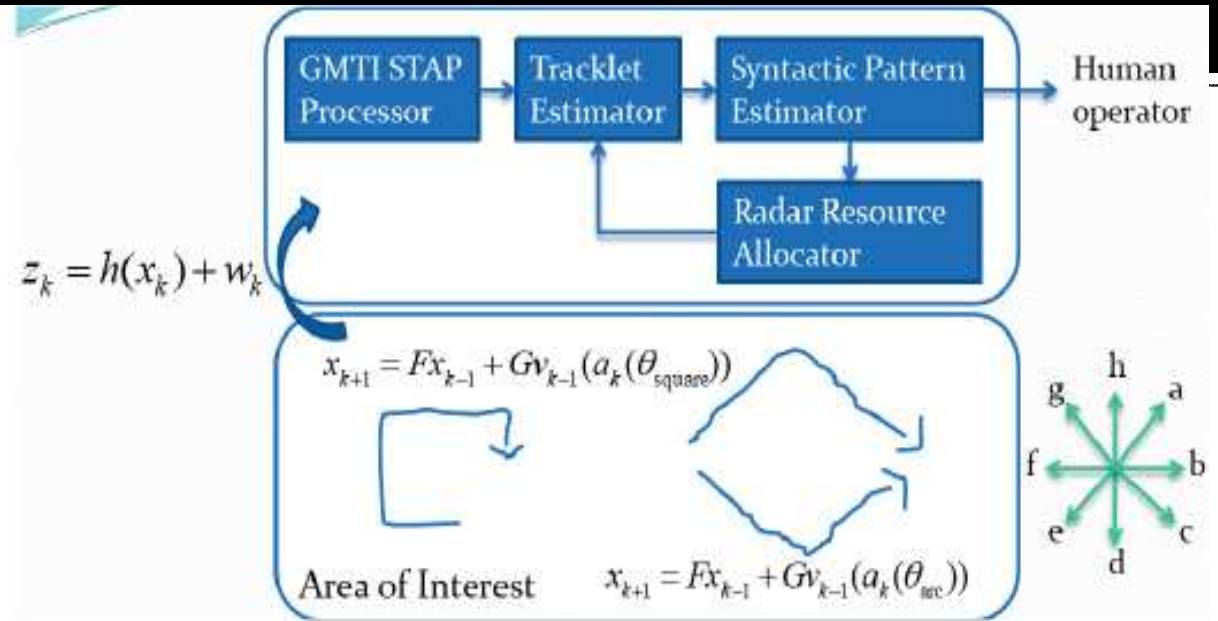
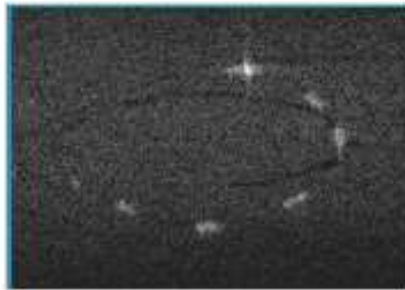
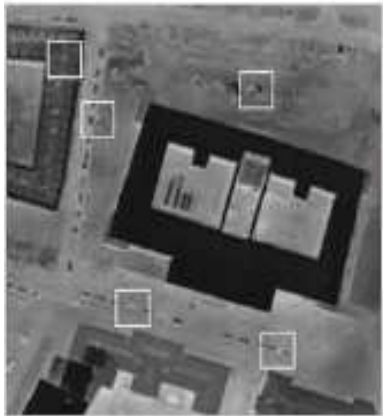


## Ex2: Destination Constrained Trajectories



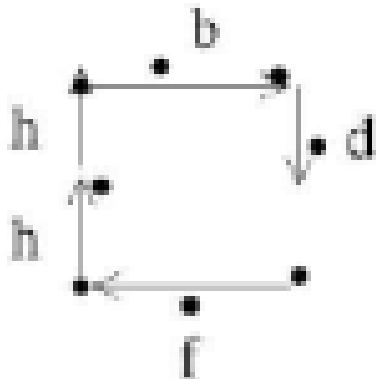
State-Space Models for target movement are for short time scales. How to model these longer time-scale trajectories? How to do Bayesian estimation?

# Main Idea: Parsimonious Models

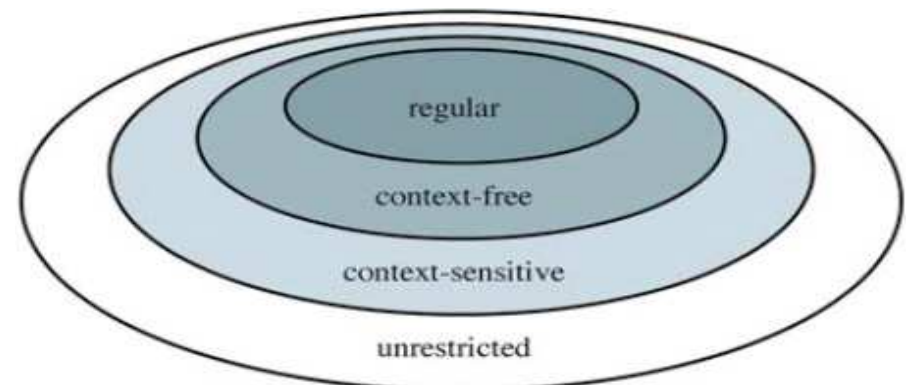


Green Zone Protection

- **How to assist human operators in intent inference?** Meta-level signal processing human-sensor interface (beyond physical sensor)
- **Key Paradigm:** (i) Stochastic Context-Free Grammar Model  
(ii) Reciprocal Markov Processes (1-dimensional Markov random fields).

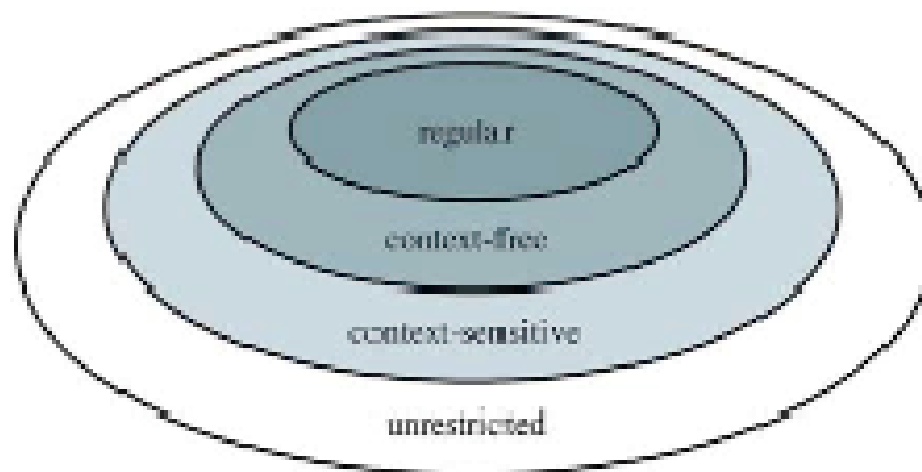


Chomsky Hierarchy  
of Formal Languages



# SCFG – Advantages

- Convenient model to capture domain knowledge of human operator
- Polynomial complexity Bayesian algorithms for estimating trajectory type (originating from Bioinformatics, Durbin, Eddy, Biological Sequence Analysis, 1998).
- Scale-invariance and Rotation-invariance (Robust)
- Efficient model (in terms of entropy) since finite state automata are a subset of context-free grammars



Begin if

....

...

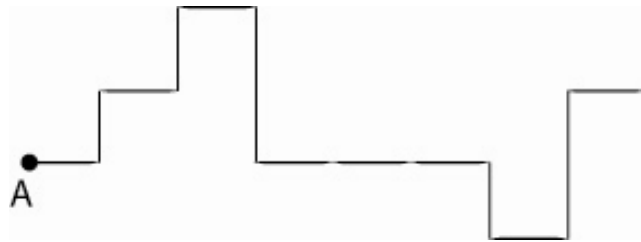
...

End if

# Trajectory Modeling – beyond Markoviana

Example 1:

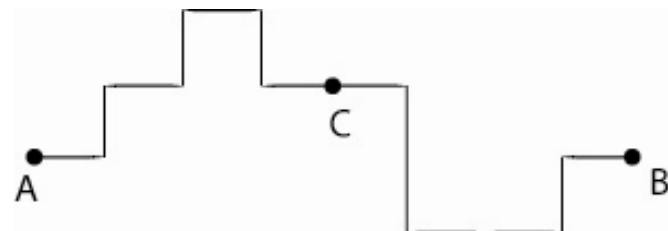
1. Random Walk



1. Markovian Bridge (goal-directed trajectory) = reciprocal process

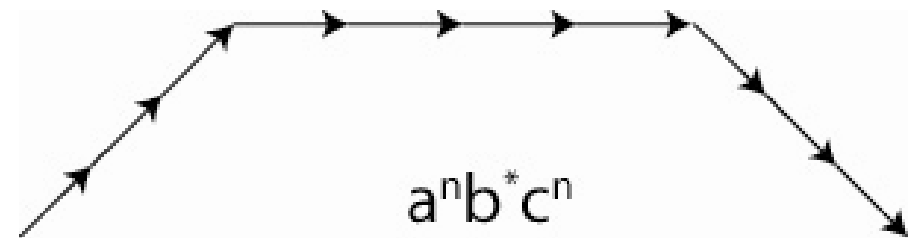


2. SCFG (allows random time between waypoints)

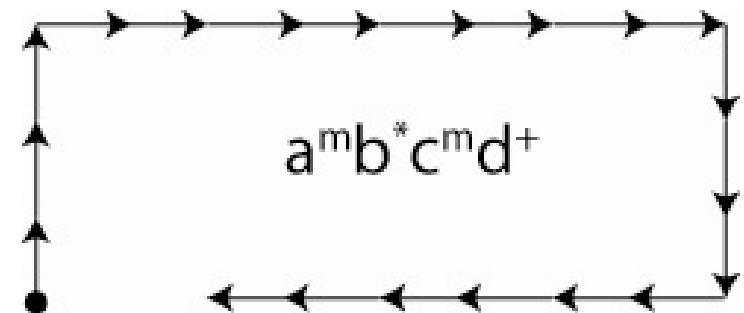


Example 2 (cannot be modeled by an HMM):

1. Arc Trajectory



2. m-Rectangle Trajectory



# SCFG vs HMM

HMM (stochastic regular grammar or automata):

$$A = \begin{bmatrix} & S_1 & S_2 \\ S_1 & 0.9 & 0.1 \\ S_2 & 0.2 & 0.8 \end{bmatrix}, B = \begin{bmatrix} & a & b \\ S_1 & 0.6 & 0.4 \\ S_2 & 0.3 & 0.7 \end{bmatrix}$$

Non terminals =  $NT = \{\text{start}, S_1, S_2\}$ ,

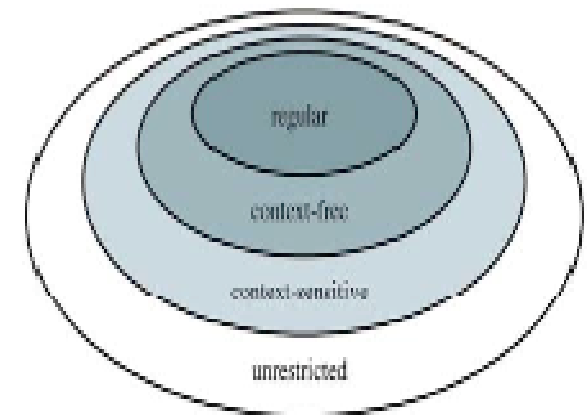
Terminals =  $T = \{a, b, \text{end}\}$ . Production rules  $P$ :

$S_1 \xrightarrow{0.54} aS_1, S_1 \xrightarrow{0.03} aS_2, S_1 \xrightarrow{0.36} bS_1, S_1 \xrightarrow{0.07} bS_2$

$S_2 \xrightarrow{0.12} aS_1, S_2 \xrightarrow{0.24} aS_2, S_2 \xrightarrow{0.08} bS_1, S_2 \xrightarrow{0.56} bS_2$

HMM strings grow linearly from left to right.

Example:  $S_1 \Rightarrow aS_2 \Rightarrow aaS_1 \Rightarrow aabS_1$



# SCFG vs HMM

**Stochastic Context Free grammar:**  $(NT, T, P)$  with

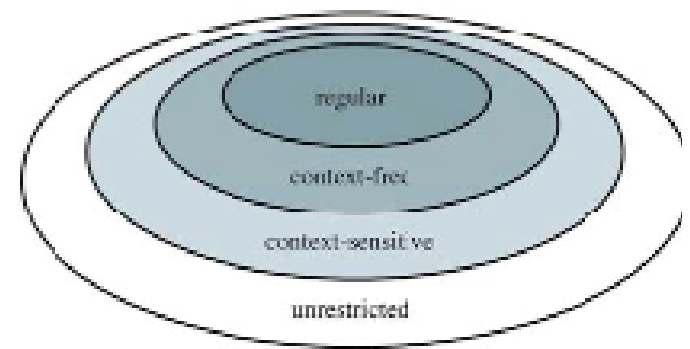
$$S_1 \xrightarrow{0.54} aS_1, S_1 \xrightarrow{0.03} aS_2, S_1 \xrightarrow{0.36} bS_1, S_1 \xrightarrow{0.07} bS_2$$

$$S_2 \xrightarrow{0.12} aS_1, S_2 \xrightarrow{0.24} aS_2, S_2 \xrightarrow{0.08} bS_1, S_2 \xrightarrow{0.3} bS_2,$$

$$\boxed{S_2 \xrightarrow{0.26} aS_2S_1} \text{ CFG strings grow inside out or on a tree}$$

Example:

$$S_1 \Rightarrow aS_2 \Rightarrow aS_2S_1 \Rightarrow aS_2aS_1 \Rightarrow aaS_2S_1abS_2$$



## Remarks:

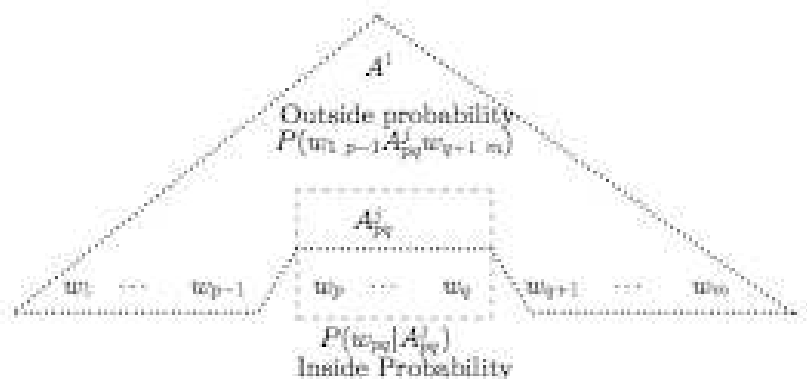
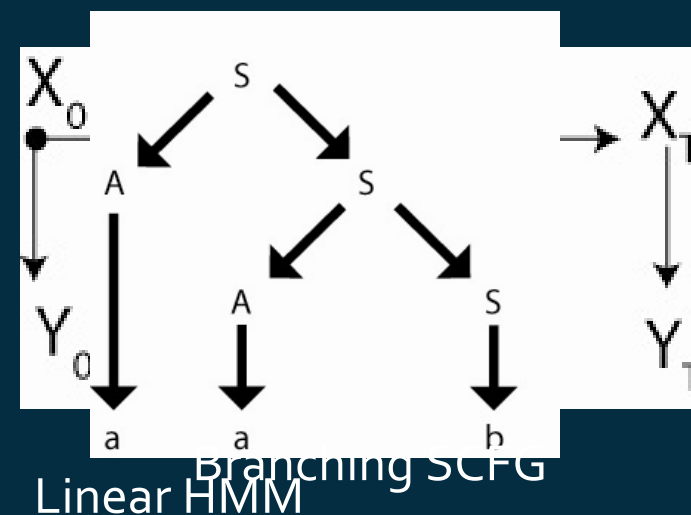
1. SCFGs are Multi-type Galton Watson Branching processes where the order matters – each realization is a tree (Directed acyclic graph).
2. Realization Theory: Chomsky normal form, etc
3. Pumping Lemmas – to prove if a grammar does not belong to a particular class



# SCFG – Signal Processing Algorithms

**Syntactic Signal Processing:** Given data string (also called sequence of terminals)  $Y_T = (y_1, \dots, y_T)$   $x$  denotes state,  $N$  denotes non-terminal.

	HMM	SCFG
Forward Filter	$P(x_k, Y_{1:k})$	$P(N_{k_1:k_2}, Y_{1:k-1}, Y_{k+1:T})$
Backward Filter	$P(Y_{k+1:T}   x_k)$	$P(Y_{k_1:k_2} N   k_1:k_2)$
MAP	Viterbi	Earley Stolcke Parser or Cocke-Younger-Kasami
EM alg	Forward/backward	Inside Outside



SCFG Bayesian estimation is polynomial complexity – cubic in data length.



# An Arc Trajectory ( $a^n b^+ c^n$ )

## VELOCITY TRACKLETS

$S \rightarrow AXC$

$S \rightarrow ABC \rightarrow \frac{3\pi}{4} BC$

$\rightarrow \frac{3\pi}{4} \pi BC$

$\rightarrow \frac{3\pi}{4} \pi \pi C$

$\rightarrow \frac{3\pi}{4} \pi \pi \frac{5\pi}{4}$

## GRAMMAR RULES

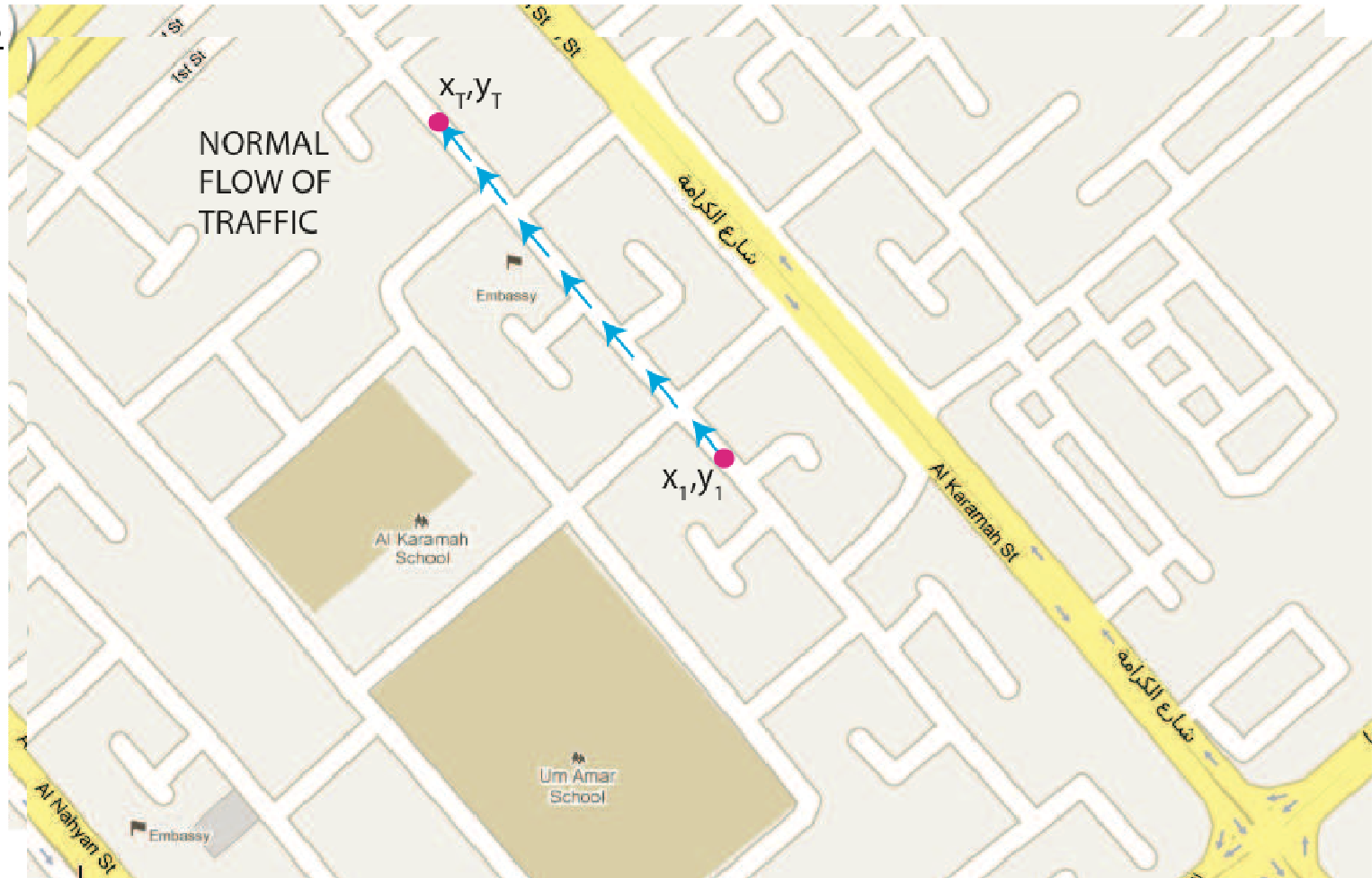
$S \rightarrow AXC$

$X \rightarrow AXC | ABC | B$

$A \rightarrow \frac{3\pi}{4}$

$B \rightarrow \pi B | \pi$

$C \rightarrow \frac{5\pi}{4}$



# Summary and References

1. Syntactic Models allow for complex trajectories – work seamlessly with legacy trackers.
2. Polynomial complexity Bayesian stochastic parsing (filtering) algorithms
3. Human—sensor interface – SCFG parsing assists human in intent inference.
4. System-theoretic issues: Sub-criticality (polynomial stability); Constraints.
5. Sensitivity of posterior distribution to prior.

1. Durbin, Eddie, Krogh, *Biological Sequence Analysis*, Cambridge, 1998
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3. K.S. Fu, *Syntactic Pattern Recognition*, Prentice Hall, 1982.
4. Wang, Krishnamurthy, Balaji, *Syntactic Tracking and Intent Inference for GMTI*, IEEE Trans Aerospace Electronic Systems, Jan 2012.
5. Krishnamurthy, Fanaswalla, *Intent Inference via Syntactic Tracking*, DSP, 2011 (Proc of DASP 2009)
6. Visnevski, Krishnamurthy, Haykin, *Syntactic Modeling of Multifunction Radars*, Proceedings of IEEE, 2007.

